

> restart

> SolGral := y(x) = C[1]·exp(2 x)·cos(3 x) + C[2]·exp(2 x)·sin(3 x) + 5·exp(5 x)

$$\text{SolGral} := y(x) = C_1 e^{2x} \cos(3x) + C_2 e^{2x} \sin(3x) + 5 e^{5x} \quad (1)$$

> DerSol := diff(SolGral, x)

$$\text{DerSol} := \frac{d}{dx} y(x) = 2 C_1 e^{2x} \cos(3x) - 3 C_1 e^{2x} \sin(3x) + 2 C_2 e^{2x} \sin(3x) + 3 C_2 e^{2x} \cos(3x) + 25 e^{5x} \quad (2)$$

> DerSegSol := diff(DerSol, x)

$$\text{DerSegSol} := \frac{d^2}{dx^2} y(x) = -5 C_1 e^{2x} \cos(3x) - 12 C_1 e^{2x} \sin(3x) - 5 C_2 e^{2x} \sin(3x) + 12 C_2 e^{2x} \cos(3x) + 125 e^{5x} \quad (3)$$

> Raiz := solve({DerSol, DerSegSol}, {C[1], C[2]}) :

> Raiz[1]

$$C_1 = -\frac{1}{39} \frac{1}{e^{2x} (\sin(3x)^2 + \cos(3x)^2)} \left(3 \left(\frac{d^2}{dx^2} y(x) \right) \cos(3x) - 75 e^{5x} \cos(3x) - 12 \cos(3x) \left(\frac{d}{dx} y(x) \right) + 2 \left(\frac{d^2}{dx^2} y(x) \right) \sin(3x) - 375 e^{5x} \sin(3x) + 5 \sin(3x) \left(\frac{d}{dx} y(x) \right) \right) \quad (4)$$

> Raiz[2]

$$C_2 = \frac{1}{39} \frac{1}{e^{2x} (\sin(3x)^2 + \cos(3x)^2)} \left(-3 \left(\frac{d^2}{dx^2} y(x) \right) \sin(3x) + 2 \left(\frac{d^2}{dx^2} y(x) \right) \cos(3x) + 75 e^{5x} \sin(3x) - 375 e^{5x} \cos(3x) + 12 \sin(3x) \left(\frac{d}{dx} y(x) \right) + 5 \cos(3x) \left(\frac{d}{dx} y(x) \right) \right) \quad (5)$$

> Ecua := isolate(simplify(subs(C[1] = rhs(Raiz[1]), C[2] = rhs(Raiz[2]), SolGral)), diff(y(x), x\$2))

$$\text{Ecua} := \frac{d^2}{dx^2} y(x) = -13 y(x) + 90 e^{5x} + 4 \left(\frac{d}{dx} y(x) \right) \quad (6)$$

> EcuaOriginal := lhs(Ecua) - (-13 y(x) + 4 (d/dx y(x))) = rhs(Ecua) - (-13 y(x) + 4 (d/dx y(x)))

$$\text{EcuaOriginal} := \frac{d^2}{dx^2} y(x) + 13 y(x) - 4 \left(\frac{d}{dx} y(x) \right) = 90 e^{5x} \quad (7)$$

> SolGral

$$y(x) = C_1 e^{2x} \cos(3x) + C_2 e^{2x} \sin(3x) + 5 e^{5x} \quad (8)$$

```

| > Comprobacion := eval(subs(y(x) = rhs(SolGral), lhs(EcuaOriginal)) - rhs(EcuaOriginal)
|   = 0)
|
| Comprobacion := 0 = 0
| >

```

(9)