

```

> restart;
> Ecua := (diff(y(x), x)) · 2 · (2 - 3 · y(x)) · 2 = 4 · (1 - y(x))
Ecua :=  $\left( \frac{dy}{dx} \right)^2 (2 - 3y(x))^2 = 4 - 4y(x)$  (1)

> Sol := dsolve(Ecua) : SolSing := Sol[1];
SolSing := y(x) = 1 (2)

> SolGral := y(x) · 2 · (1 - y(x)) = (x - C) · 2
SolGral :=  $y(x)^2 (1 - y(x)) = (x - C)^2$  (3)

> SolPart := subs(C = 5, SolGral)
SolPart :=  $y(x)^2 (1 - y(x)) = (x - 5)^2$  (4)

> DerUno := isolate(Ecua, diff(y(x), x)) · 2
DerUno :=  $\left( \frac{dy}{dx} \right)^2 = \frac{4 - 4y(x)}{(2 - 3y(x))^2}$  (5)

> DerSol := isolate(diff(SolGral, x), diff(y(x), x))
DerSol :=  $\frac{d}{dx} y(x) = \frac{2x - 2C}{2y(x)(1 - y(x)) - y(x)^2}$  (6)

> Param := isolate(DerSol, C)
Param :=  $C = -\frac{1}{2} \left( \frac{dy}{dx} \right) (2y(x)(1 - y(x)) - y(x)^2) + x$  (7)

> DerSolGral := isolate(subs(C = rhs(Param), SolGral), diff(y(x), x)) · 2
DerSolGral :=  $\left( \frac{dy}{dx} \right)^2 = \frac{4y(x)^2 (1 - y(x))}{(2y(x)(1 - y(x)) - y(x)^2)^2}$  (8)

> Comprobacion := simplify(rhs(DerUno) - rhs(DerSolGral)) = 0
Comprobacion := 0 = 0 (9)

> ComprobacionDos := eval(subs(y(x) = rhs(SolSing), Ecua))
ComprobacionDos := 0 = 0 (10)

>

> restart;
> Ecua := (1 - x^2 * y(x)) + x^2 * (y(x) - x) * diff(y(x), x) = 0;

Ecua :=  $1 - x^2 y(x) + x^2 (y(x) - x) \left( \frac{dy}{dx} \right) = 0$  (11)

> M := 1 - x^2 * y;
M :=  $-x^2 y + 1$  (12)

> N := x^2 * (y - x);

```

$$N := x^2 (y - x) \quad (13)$$

```
> with(DEtools):
> odeadvisor(Ecua);
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$$[_{\text{rational}}, [_{\text{1st_order}}, _{\text{with_symmetry}}[F(x), G(x)]], [_{\text{Abel}}, 2\text{nd type, class } B]] \quad (14)$$

```
> FI:=intfactor(Ecua);
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$$FI := \frac{1}{x^2} \quad (15)$$

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> MM:=expand(FI*M);
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$$MM := -y + \frac{1}{x^2} \quad (16)$$

```
> NN:=expand(FI*N);
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$$NN := y - x \quad (17)$$

```
> Comprobacion:=diff(MM,y)-diff(NN,x)=0;
```

$$\text{Comprobacion} := 0 = 0 \quad (18)$$

```
> IntMMx:=Int(MM,x);
```

$$\text{IntMMx} := \int \left(-y + \frac{1}{x^2} \right) dx \quad (19)$$

```
> IntMMx:=int(MM,x);
```

$$\text{IntMMx} := -x y - \frac{1}{x} \quad (20)$$

```
> SolGral:=IntMMx+Int((NN-diff(IntMMx,y)),y)=C1;
```

$$\text{SolGral} := -x y - \frac{1}{x} + \int y dy = C1 \quad (21)$$

```
> SolGral:=IntMMx+int((NN-diff(IntMMx,y)),y)=C1;
```

$$\text{SolGral} := -x y - \frac{1}{x} + \frac{y^2}{2} = C1 \quad (22)$$

```
> Ecua;
```

$$1 - x^2 y(x) + x^2 (y(x) - x) \left(\frac{d}{dx} y(x) \right) = 0 \quad (23)$$

```
> SolGralDos:=-x*y(x)-1/x+1/2*y(x)^2 = C1;
```

$$(24)$$

$$SolGralDos := -x y(x) - \frac{1}{x} + \frac{1}{2} y(x)^2 = CI \quad (24)$$

```
> DerivSol:=diff(SolGralDos,x);
```

$$DerivSol := -y(x) - x \left(\frac{d}{dx} y(x) \right) + \frac{1}{x^2} + y(x) \left(\frac{d}{dx} y(x) \right) = 0 \quad (25)$$

> Ecua;

$$1 - x^2 y(x) + x^2 (y(x) - x) \left(\frac{d}{dx} y(x) \right) = 0 \quad (26)$$

```
> DespUno:=isolate(DerivSol,diff(y(x),x));
```

$$DespUno := \frac{d}{dx} y(x) = \frac{y(x) - \frac{1}{x^2}}{y(x) - x} \quad (27)$$

```
> DespDos:=isolate(Ecua,diff(y(x),x));
```

$$DespDos := \frac{d}{dx} y(x) = \frac{-1 + x^2 y(x)}{x^2 (y(x) - x)} \quad (28)$$

```
> Comprobacion:=simplify(rhs(DespUno)-rhs(DespDos))=0;
```

$$Comprobacion := 0 = 0 \quad (29)$$

_> restart;

```
> Ecua:=diff(x(t),t$2)+2*diff(x(t),t)+x(t)=3*exp(-t)+4*t*exp(-t);
```

$$Ecua := \frac{d^2}{dt^2} x(t) + 2 \left(\frac{d}{dt} x(t) \right) + x(t) = 3 e^{-t} + 4 t e^{-t} \quad (30)$$

```
> EcuaHom:=lhs(Ecua)=0;
```

$$EcuaHom := \frac{d^2}{dt^2} x(t) + 2 \left(\frac{d}{dt} x(t) \right) + x(t) = 0 \quad (31)$$

```
> Q:=rhs(Ecua);
```

$$O := 3 e^{-t} + 4 t e^{-t} \quad (32)$$

> EcuaCarac := $m^{*}2+2*m+1=0;$

$$EcuaCarac := m^2 + 2m + 1 = 0 \quad (33)$$

```
> Raiz:=solve(EcuaCarac);
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$$Raiz := -1, -1 \quad (34)$$

```
> x1:=exp(Raiz[1]*t);
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$$x_1 := e^{-t} \quad (35)$$

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> x2:=t*exp(Raiz[1]*t);
```

$$x_2 \equiv t e^{-t} \quad (36)$$

> Sol:=x(t)=C1*x1+C2*x2;

$$xz : \quad \text{in } \mathbb{C} \quad \quad \quad (36)$$

> Sol:=x(t)=C1*x1+C2*x2;

(37)

$$Sol := x(t) = C1 e^{-t} + C2 t e^{-t} \quad (37)$$

```
> SolNoHom:=x(t)=A*x1+B*x2;
      SolNoHom := x(t) = A e^{-t} + B t e^{-t} \quad (38)
```

```
> with(linalg):
> WW:=wronskian([x1,x2],t);
      WW := \begin{bmatrix} e^{-t} & t e^{-t} \\ -e^{-t} & e^{-t} - t e^{-t} \end{bmatrix} \quad (39)
```

```
> ZZ:=array([0,Q]);
      ZZ := \begin{bmatrix} 0 & 3 e^{-t} + 4 t e^{-t} \end{bmatrix} \quad (40)
```

```
> Param:=linsolve(WW,ZZ);
      Param := \begin{bmatrix} -t (4 t + 3) & 4 t + 3 \end{bmatrix} \quad (41)
```

```
> Aprima:=Param[1];
      Aprima := -t (4 t + 3) \quad (42)
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```
> Bprima:=Param[2];
      Bprima := 4 t + 3 \quad (43)
```

```
> A:=int(Aprima,t)+C1;B:=int(Bprima,t)+C2;
      A := -\frac{4}{3} t^3 - \frac{3}{2} t^2 + C1 \quad (44)
```

$$B := 2 t^2 + C2 + 3 t$$

```
> SolSol:=expand(SolNoHom);
      SolSol := x(t) = \frac{2}{3} \frac{t^3}{e^t} + \frac{3}{2} \frac{t^2}{e^t} + \frac{C1}{e^t} + \frac{t C2}{e^t} \quad (45)
```

```
> SolPart:=subs(C1=1,C2=2,SolSol);
> SolPartDos:=subs(C1=2,C2=1,SolSol);
      SolPart := x(t) = \frac{2}{3} \frac{t^3}{e^t} + \frac{3}{2} \frac{t^2}{e^t} + \frac{1}{e^t} + \frac{2 t}{e^t} \quad (46)
```

$$SolPartDos := x(t) = \frac{2}{3} \frac{t^3}{e^t} + \frac{3}{2} \frac{t^2}{e^t} + \frac{2}{e^t} + \frac{t}{e^t}$$

```
> plot([rhs(SolPart),rhs(SolPartDos),rhs(diff(SolPart,t)),rhs(diff(SolPartDos,t))),t=0..10);
```

