

> restart

$$\begin{aligned}> EcuaDerParc &:= \text{diff}(z(x, y), x\$2) - 8 \cdot \text{diff}(z(x, y), y) = 0 \\ EcuaDerParc &:= \frac{\partial^2}{\partial x^2} z(x, y) - 8 \left(\frac{\partial}{\partial y} z(x, y) \right) = 0\end{aligned}\quad (1)$$

> with(PDEtools) :

> pdsolve(EcuaDerParc)

$$\begin{aligned}(z(x, y) = _F1(x) _F2(y)) \&\text{where } \left[\left\{ \frac{d^2}{dx^2} _F1(x) = _c_1 _F1(x), \frac{d}{dy} _F2(y) \right. \right. \\ &= \frac{1}{8} _c_1 _F2(y) \left. \right\} \left. \right]\end{aligned}\quad (2)$$

> SolDerParc := build(%)

$$SolDerParc := z(x, y) = e^{\sqrt{-c_1} x} _C3 e^{\frac{1}{8} -c_1 y} _C1 + \frac{-C3 e^{\frac{1}{8} -c_1 y} _C2}{e^{\sqrt{-c_1} x}}\quad (3)$$

> restart

$$\begin{aligned}> EcuaDerParc &:= \text{diff}(z(x, y), x\$2) - 8 \cdot \text{diff}(z(x, y), y) = 0 \\ EcuaDerParc &:= \frac{\partial^2}{\partial x^2} z(x, y) - 8 \left(\frac{\partial}{\partial y} z(x, y) \right) = 0\end{aligned}\quad (4)$$

> Ecua := subs(z(x, y) = F(x) · G(y), EcuaDerParc)

$$Ecua := \frac{\partial^2}{\partial x^2} (F(x) G(y)) - 8 \left(\frac{\partial}{\partial y} (F(x) G(y)) \right) = 0\quad (5)$$

$$\begin{aligned}> EcuaDos &:= \text{lhs}(Ecua) - \left(-8 \left(\frac{\partial}{\partial y} (F(x) G(y)) \right) \right) = \text{rhs}(Ecua) - \left(-8 \left(\frac{\partial}{\partial y} (F(x) G(y)) \right) \right)\end{aligned}$$

$$EcuaDos := \left(\frac{d^2}{dx^2} F(x) \right) G(y) = 8 F(x) \left(\frac{d}{dy} G(y) \right)\quad (6)$$

$$> EcuaTres := \frac{\text{lhs}(EcuaDos)}{F(x) · G(y)} = \frac{\text{rhs}(EcuaDos)}{F(x) · G(y)}$$

$$EcuaTres := \frac{\frac{d^2}{dx^2} F(x)}{F(x)} = \frac{8 \left(\frac{d}{dy} G(y) \right)}{G(y)}\quad (7)$$

> EcuaX := lhs(EcuaTres) = a; EcuaY := rhs(EcuaTres) = a

$$EcuaX := \frac{\frac{d^2}{dx^2} F(x)}{F(x)} = a$$

$$EcuaY := \frac{8 \left(\frac{d}{dy} G(y) \right)}{G(y)} = a\quad (8)$$

> SolXcero := dsolve(subs(a = 0, EcuaX))

$$SolXcero := F(x) = _C1 x + _C2\quad (9)$$

```

> SolYcero := dsolve(subs(a=0, EcuaY) )
          SolYcero := G(y) = _C1
(10)

> SolGralCero := z(x,y) = rhs(SolXcero) · (subs(_C1=1, rhs(SolYcero)) )
          SolGralCero := z(x,y) = _C1 x + _C2
(11)

> SolXpos := dsolve(subs(a=b·2, EcuaX) )
          SolXpos := F(x) = _C1 e-bx + _C2 ebx
(12)

> SolYpos := dsolve(subs(a=b·2, EcuaY) )
          SolYpos := G(y) = _C1 e $\frac{1}{8} b^2 y$ 
(13)

> SolGralPos := z(x,y) = rhs(SolXpos) · (subs(_C1=1, rhs(SolYpos)) )
          SolGralPos := z(x,y) = (_C1 e-bx + _C2 ebx) e $\frac{1}{8} b^2 y$ 
(14)

> SolXneg := dsolve(subs(a=-b·2, EcuaX) )
          SolXneg := F(x) = _C1 sin(b x) + _C2 cos(b x)
(15)

> SolYneg := dsolve(subs(a=-b·2, EcuaY) )
          SolYneg := G(y) = _C1 e $-\frac{1}{8} b^2 y$ 
(16)

> SolGralNeg := z(x,y) = rhs(SolXneg) · (subs(_C1=1, rhs(SolYneg)) )
          SolGralNeg := z(x,y) = (_C1 sin(b x) + _C2 cos(b x)) e $-\frac{1}{8} b^2 y$ 
(17)

> restart
> EcuaDerParc := diff(z(x,y), x$2) - 4·diff(z(x,y), y) = z(x,y)
          EcuaDerParc :=  $\frac{\partial^2}{\partial x^2} z(x,y) - 4 \left( \frac{\partial}{\partial y} z(x,y) \right) = z(x,y)$ 
(18)

> Ecua := eval(subs(z(x,y)=F(x)·G(y), EcuaDerParc) )
          Ecua :=  $\left( \frac{d^2}{dx^2} F(x) \right) G(y) - 4 F(x) \left( \frac{d}{dy} G(y) \right) = F(x) G(y)$ 
(19)

> EcuaUno := lhs(Ecua) -  $\left( -4 F(x) \left( \frac{d}{dy} G(y) \right) \right) = rhs(Ecua) - \left( -4 F(x) \left( \frac{d}{dy} G(y) \right) \right)$ 
          EcuaUno :=  $\left( \frac{d^2}{dx^2} F(x) \right) G(y) = F(x) G(y) + 4 F(x) \left( \frac{d}{dy} G(y) \right)$ 
(20)

> EcuaUnoUno :=  $\frac{lhs(EcuaUno)}{F(x) \cdot G(y)} = simplify \left( \frac{rhs(EcuaUno)}{F(x) \cdot G(y)} \right)$ 
          EcuaUnoUno :=  $\frac{\frac{d^2}{dx^2} F(x)}{F(x)} = \frac{G(y) + 4 \left( \frac{d}{dy} G(y) \right)}{G(y)}$ 
(21)

> EcuaDos := lhs(Ecua) -  $\left( -4 F(x) \left( \frac{d}{dy} G(y) \right) + F(x) \cdot G(y) \right) = rhs(Ecua) - \left( -4 F(x) \left( \frac{d}{dy} G(y) \right) + F(x) \cdot G(y) \right)$ 
          EcuaDos :=  $\left( \frac{d^2}{dx^2} F(x) \right) G(y) - F(x) G(y) = 4 F(x) \left( \frac{d}{dy} G(y) \right)$ 
(22)

```

$$\begin{aligned} > EcuaDosUno := \text{simplify}\left(\frac{\text{lhs}(EcuaDos)}{F(x) \cdot G(y)}\right) = \text{simplify}\left(\frac{\text{rhs}(EcuaDos)}{F(x) \cdot G(y)}\right) \\ & EcuaDosUno := -\frac{F(x) - \left(\frac{d^2}{dx^2} F(x)\right)}{F(x)} = \frac{4 \left(\frac{d}{dy} G(y)\right)}{G(y)} \end{aligned} \quad (23)$$

$$\begin{aligned} > \text{with(PDEtools)} : \\ > SolGral := \text{pdsolve}(EcuaDerParc) \\ SolGral := (z(x, y) = _F1(x) _F2(y)) \& \text{where } \left[\left\{ \frac{d^2}{dx^2} _F1(x) = _c_1 _F1(x), \frac{d}{dy} _F2(y) \right. \right. \\ & \left. \left. = \frac{1}{4} _c_1 _F2(y) - \frac{1}{4} _F2(y) \right\} \right] \end{aligned} \quad (24)$$

$$\begin{aligned} > SolGralFinal := \text{build}(SolGral) \\ SolGralFinal := z(x, y) = e^{\sqrt{-c_1} x} _C3 e^{\frac{1}{4} y - c_1} e^{-\frac{1}{4} y} _C1 + \frac{e^{\frac{1}{4} y - c_1} e^{-\frac{1}{4} y} _C2}{e^{\sqrt{-c_1} x}} \end{aligned} \quad (25)$$

$$\begin{aligned} > Comprobacion := \text{eval}(\text{subs}(z(x, y) = \text{rhs}(SolGralFinal), \text{lhs}(EcuaDerParc) \\ & - \text{rhs}(EcuaDerParc) = 0)) \\ Comprobacion := 0 = 0 \end{aligned} \quad (26)$$