

EDOL



Solución  $y = GY_1 + Y_p$

función explícita

`dsolve( )`

EDO NL

$$M + N \frac{dy}{dx} = 0$$

$$\int F(x, y) = C_1$$

función implícita

`with(DEtools)`

EJERCICIOS

$$(xy^2 - y^3 + x - 1) + (x^2y - 2xy + x^2 + 2y - 2x + 2) \frac{dy}{dx} = 0$$

$M$        $\uparrow$        $N$        $\uparrow$

$$M + N \frac{dy}{dx} = 0$$

↓

$$P(x)Q(y) + R(x)S(y) \frac{dy}{dx} = 0$$

Sol  
genal

$$\int \frac{P(x)}{R(x)} dx + \int \frac{S(y)}{Q(y)} dy = C_1$$

$$F(x, y) = C$$

$$\frac{\partial F}{\partial x} + \frac{\partial F}{\partial y} \cdot \frac{dy}{dx} = 0$$

$$e^y(1+x^2) \frac{dy}{dx} - 2x(1+e^y) = 0$$

$$F(x, y) = C_1$$

SOL  
GRAL

$$M + N \frac{dy}{dx} = 0$$

$$F(x,y) = C_1$$

$$\frac{\partial F}{\partial x} + \frac{\partial F}{\partial y} \cdot \frac{dy}{dx} = 0$$

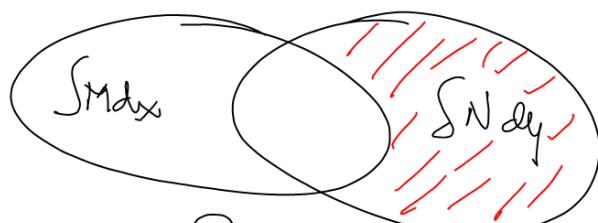
$$\frac{\partial^2 F}{\partial y \partial x} = \frac{\partial^2 F}{\partial x \partial y}$$

$$M = \frac{\partial F}{\partial x}, \quad N = \frac{\partial F}{\partial y}$$

$$\frac{\partial M}{\partial y} = \frac{\partial N}{\partial x}$$


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$$\int M dx \cup \int N dy = C_1$$



Sg  
Existe

$$\int M dx + \int \left[ N - \frac{\partial}{\partial y} \int M dx \right] dy = C_1$$

$$(x^3 + xy^2) + (x^2y + y^3) \frac{dy}{dx} = 0$$

M                    N

$$\frac{\partial M}{\partial y} = 2xy$$

$$\frac{\partial N}{\partial x} = 2xy$$

$$\int M dx = \int x^3 dx + y^2 \int x dx$$

$$= \frac{x^4}{4} + y^2 \frac{x^2}{2}$$

$$\frac{\partial}{\partial y} \left( \int M dx \right) = 4x^2$$

$$\left[ N - \frac{\partial}{\partial y} \left( \int M dx \right) \right] = x^2 y + y^3 - 4x^2$$

$$\int \left[ N - \frac{\partial}{\partial y} \left( \int M dx \right) \right] dy = \int y^3 dy$$

Sol.  
gen.

$$\frac{x^4}{4} + \frac{x^2 y^2}{2} + \frac{y^4}{4} = C_1$$