

ED en DP.

$$\frac{\partial^2 z}{\partial x^2} + 4 \frac{\partial^2 z}{\partial x \partial y} + 4 \frac{\partial^2 z}{\partial y^2} = 0$$

$$z(x, y) = f(y + mx) \quad \left| \quad \begin{array}{l} z(x, y) = f(u) \\ u = y + mx \end{array} \right.$$

$$\frac{\partial z}{\partial x} = m f' \quad \frac{\partial z}{\partial y} = f'$$

$$\frac{\partial^2 z}{\partial x^2} = m^2 f'' \quad \frac{\partial^2 z}{\partial x \partial y} = m f'' \quad \frac{\partial^2 z}{\partial y^2} = f''$$

$$m^2 f'' + 4m f'' + 4f'' = 0$$

$$(m^2 + 4m + 4) f'' = 0 \quad f'' = 0 \quad f' = k_1 \quad \boxed{f = k_1(y + mx) + k_2}$$

$$\left. \begin{array}{l} m^2 + 4m + 4 = 0 \\ (m + 2)^2 = 0 \\ m_1 = m_2 = -2 \end{array} \right\} f_1(y - 2x) \quad \text{TRIVIAL}$$

$$z(x, y) = f_1(y - 2x) + x f_2(y - 2x)$$

$$z(x, y) = f_1(y - 2x) + y f_2(y - 2x).$$

$$\frac{\partial^2 U(x, y, z)}{\partial x^2} + \frac{\partial^2 U(x, y, z)}{\partial z^2} + \frac{\partial^2 U(x, y, z)}{\partial y^2} = 0$$

$$U(x, y, z) = F(x) \cdot G(y, z)$$

$$\frac{F''(x)}{F(x)} = \frac{\frac{\partial G}{\partial y} \cdot \frac{\partial G}{\partial z}}{y+z}.$$

