

```
> restart
```

```
> F :=  $\frac{s}{s^2 + s + 1}$ 
```

$$F := \frac{s}{s^2 + s + 1} \quad (1)$$

```
> with(inttrans) :
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```
> f := expand(invlaplace(F, s, t))
```

$$f := e^{-\frac{1}{2}t} \cos\left(\frac{1}{2}\sqrt{3}t\right) - \frac{1}{3}e^{-\frac{1}{2}t}\sqrt{3}\sin\left(\frac{1}{2}\sqrt{3}t\right) \quad (2)$$

```
> FF := laplace(f, t, s)
```

$$FF := \frac{s}{s^2 + s + 1} \quad (3)$$

```
> restart
```

```
> Ecua := y'' + 3y' + 2y = 2 \cdot \exp(4 \cdot x) + x^3 + \sin(2 \cdot x)
```

$$Ecua := \frac{d^2}{dx^2} y(x) + 3 \left( \frac{d}{dx} y(x) \right) + 2y(x) = 2e^{4x} + x^3 + \sin(2x) \quad (4)$$

```
> CondIni := y(0) = 4, D(y)(0) = -6
```

$$CondIni := y(0) = 4, D(y)(0) = -6 \quad (5)$$

```
> with(inttrans) :
```

```
> EcuaTL := subs(\{CondIni\}, \{laplace(Ecua, x, s)\})
```

$$\begin{aligned} EcuaTL &:= \left\{ s^2 \text{laplace}(y(x), x, s) - 6 - 4s + 3s \text{laplace}(y(x), x, s) + 2 \text{laplace}(y(x), x, s) \right. \\ &\quad \left. = \frac{2}{s-4} + \frac{6}{s^4} + \frac{2}{s^2+4} \right\} \end{aligned} \quad (6)$$

```
> SolTL := expand(isolate(EcuaTL[1], laplace(y(x), x, s)))
```

$$\begin{aligned} SolTL &:= \text{laplace}(y(x), x, s) = \frac{2}{(s^2 + 3s + 2)(s-4)} + \frac{6}{(s^2 + 3s + 2)s^4} \\ &\quad + \frac{2}{(s^2 + 3s + 2)(s^2 + 4)} + \frac{4s}{s^2 + 3s + 2} + \frac{6}{s^2 + 3s + 2} \end{aligned} \quad (7)$$

```
> SolPart := invlaplace(SolTL, s, x)
```

$$\begin{aligned} SolPart &:= y(x) = \frac{41}{24}e^{-2x} + 8e^{-x} + \frac{1}{15}e^{4x} - \frac{45}{8} - \frac{9}{4}x^2 + \frac{1}{2}x^3 + \frac{21}{4}x - \frac{3}{20}\cos(2x) \\ &\quad - \frac{1}{20}\sin(2x) \end{aligned} \quad (8)$$

```
> Comprobar := eval(subs(y(x) = rhs(SolPart), lhs(Ecua) - rhs(Ecua) = 0))
```

$$Comprobar := 0 = 0 \quad (9)$$

```
> ComprobarDos := y(0) = simplify(subs(x=0, rhs(SolPart)))
```

$$ComprobarDos := y(0) = 4 \quad (10)$$

```
> CondIni[1]
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$$y(0) = 4 \quad (11)$$

```
> ComprobarTres := D(y)(0) = simplify(subs(x=0, rhs(diff(SolPart, x))))
```

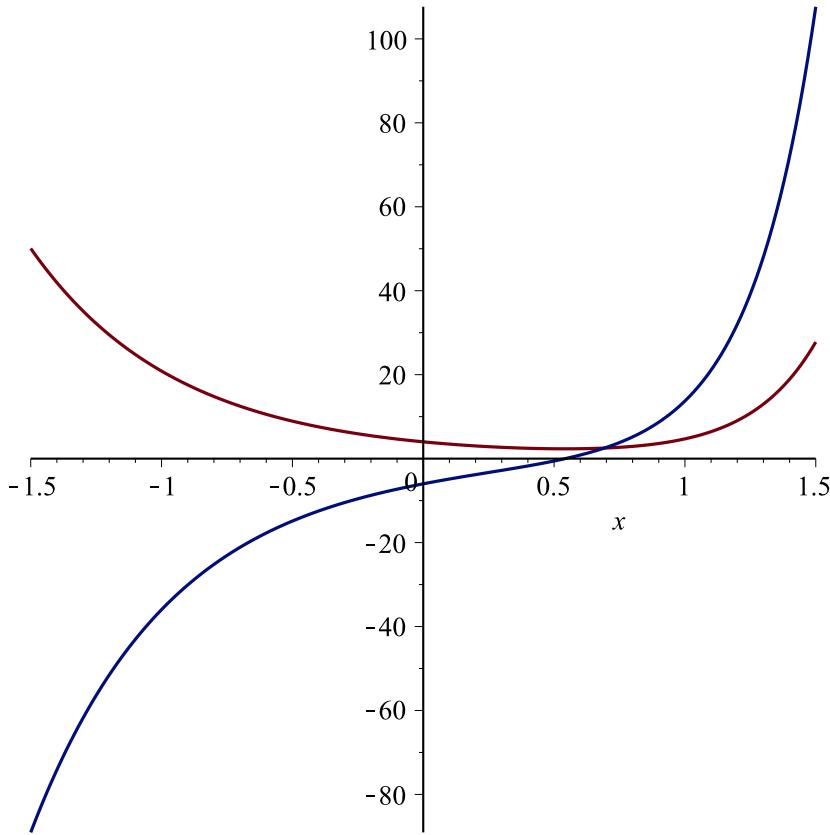
... .

$$\text{ComprobarTres} := \text{D}(y)(0) = -6 \quad (12)$$

>  $\text{CondIni}[2]$

$$\text{D}(y)(0) = -6 \quad (13)$$

>  $\text{plot}([\text{rhs}(\text{SolPart}), \text{rhs}(\text{diff}(\text{SolPart}, x))], x = -1.5 .. 1.5)$



>  $\text{restart}$   
>  $\text{Ecua} := 3 \cdot \text{diff}(i(t), t) + 10 \cdot i(t) = \text{Heaviside}(t - 2) \cdot 120 \cdot \cos(60 \cdot \text{Pi} \cdot t)$   
 $\text{Ecua} := 3 \left( \frac{d}{dt} i(t) \right) + 10 i(t) = 120 \text{Heaviside}(t - 2) \cos(60 \pi t) \quad (14)$

>  $\text{CondIni} := i(0) = 0$

$$\text{CondIni} := i(0) = 0 \quad (15)$$

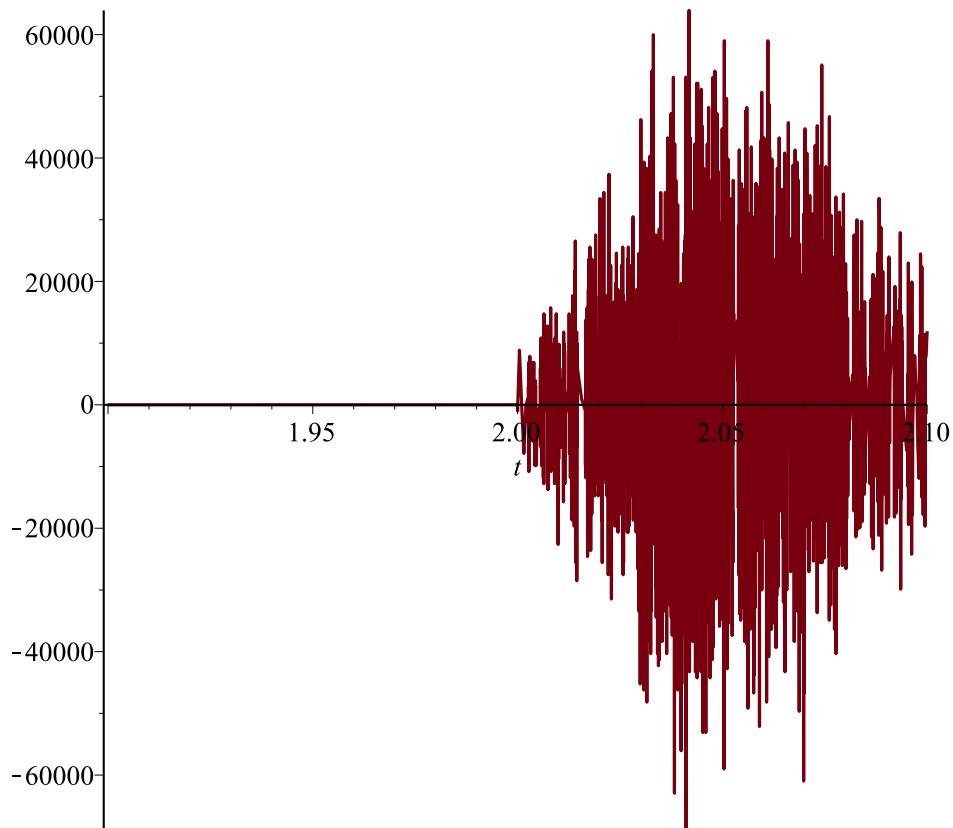
>  $\text{with(inttrans)}$  :  
>  $\text{EcuaTL} := \text{subs}(\text{CondIni}, \text{laplace}(\text{Ecua}, t, s))$

$$\text{EcuaTL} := 3 s \text{laplace}(i(t), t, s) + 10 \text{laplace}(i(t), t, s) = \frac{120 e^{-2s} s}{3600 \pi^2 + s^2} \quad (16)$$

>  $\text{SolTL} := \text{isolate}(\text{EcuaTL}, \text{laplace}(i(t), t, s))$

$$\text{SolTL} := \text{laplace}(i(t), t, s) = \frac{120 e^{-2s} s}{(3600 \pi^2 + s^2) (3 s + 10)} \quad (17)$$

```
|> SolPart := simplify(invlaplace(SolTL, s, t)) :  
|> plot(rhs(SolPart), t = 1.9 .. 2.1)
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|>
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