

$$V_c = \frac{1}{C} \int_0^t I_2(z) dz$$

$$I_2 = C \frac{dV_c}{dt}$$

$$E(t) = 120 \cos(60(2\pi)t)$$

$$\left. \begin{array}{l} R_1 = 1 \text{ ohm} \\ L = 10 \text{ henry} \\ C = \frac{1}{10} \text{ Farad} \\ R_2 = 3 \text{ ohm} \end{array} \right\} \begin{array}{l} I_1(0) = 0 \\ I_2(0) = 0 \end{array}$$

$$E(t) = V_{R_1} + V_C$$

$$E(t) = R_1 I_1(t) + V_C$$

$$I_1(t) = I_C + I_L$$

$$= C \frac{dV_C}{dt} + I_L$$

$$E(t) = R_1 \left( C \frac{dV_C}{dt} + I_L \right) + V_C$$

$$R_1 C \frac{dV_C}{dt} = -R_1 I_L - V_C + E(t)$$

$$\Rightarrow \frac{dV_C}{dt} = -\frac{1}{C} I_L - \frac{1}{R_1 C} V_C + \frac{1}{R_1 C} E(t)$$

$$V_C = V_L + V_{R_2}$$

$$V_C = L \frac{dI_L}{dt} + R_2 I_L$$

$$\Rightarrow \frac{dI_L}{dt} = \frac{1}{L} V_C - \frac{R_2}{L} I_L$$

$$V_C(0) = 0$$

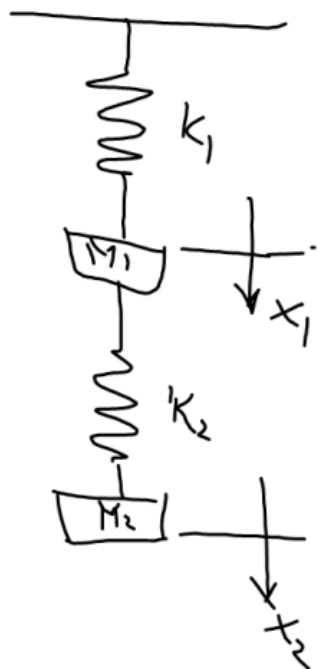
$$I_L(0) = 0$$

$$\frac{dV_C}{dt} = -10 V_C - 10 I_L + 120 \cos(120\pi t)$$

$$\frac{dI_L}{dt} = \frac{1}{10} V_C - \frac{3}{10} I_L$$

$$\frac{d}{dt} \begin{bmatrix} V_C \\ I_L \end{bmatrix} = \begin{bmatrix} -10 & -10 \\ \frac{1}{10} & -\frac{3}{10} \end{bmatrix} \begin{bmatrix} V_C \\ I_L \end{bmatrix} + \begin{bmatrix} 120 \cos(120\pi t) \\ 0 \end{bmatrix}$$

$$\bar{X} = e^{At} \bar{X}(0) + \int_0^t e^{A(t-z)} \bar{b}(z) dz$$



$$M_1 \frac{d^2 x_1(t)}{dt^2} = -k_1 x_1(t) + k_2 (x_2(t) - x_1(t))$$

$$M_2 \frac{d^2 x_2(t)}{dt^2} = -k_2 (x_2(t) - x_1(t))$$

$$x_1(0) = \frac{1}{10} \quad x_2(0) = \frac{1}{10}$$

$$\frac{dx_1}{dt}(0) = 0 \quad \frac{dx_2}{dt}(0) = 0$$

$$\frac{dx_1}{dt} = U_1(t) \quad \frac{dx_2}{dt} = U_2(t)$$

$$\dot{X} = \begin{bmatrix} x_1 \\ x_2 \\ v_1 \\ v_2 \end{bmatrix}$$

$$\frac{dx_1}{dt} = U_1(t)$$

$$\frac{dx_2}{dt} = U_2(t)$$

$$\frac{dv_1}{dt} = \frac{1}{M_1} (-k_1 - k_2) x_1(t) + \frac{k_2}{M_1} x_2(t)$$

$$\frac{dv_2}{dt} = \frac{k_2}{M_2} x_1(t) - \frac{k_2}{M_2} x_2(t)$$

