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> restart
> Ecua := y''+ 4 y' - 5 y = 0

$$Ecua := \frac{d^2}{dx^2} y(x) + 4 \left( \frac{d}{dx} y(x) \right) - 5 y(x) = 0 \quad (1)$$

> EcuaCarac := m2 + 4·m - 5 = 0

$$EcuaCarac := m^2 + 4 m - 5 = 0 \quad (2)$$

> Raiz := solve(EcuaCarac)

$$Raiz := 1, -5 \quad (3)$$

> yy[1] := exp(Raiz[1]·x); yy[2] := exp(Raiz[2]·x)

$$\begin{aligned} yy_1 &:= e^x \\ yy_2 &:= e^{-5x} \end{aligned} \quad (4)$$

> SolGral := y(x) = _C1·yy[1] + _C2·yy[2]

$$SolGral := y(x) = _C1 e^x + _C2 e^{-5x} \quad (5)$$

> with(linalg):
> WW := wronskian([yy[1], yy[2]], x)

$$WW := \begin{bmatrix} e^x & e^{-5x} \\ e^x & -5 e^{-5x} \end{bmatrix} \quad (6)$$

> comprobacion := det(WW) ≠ 0

$$comprobacion := -6 e^x e^{-5x} ≠ 0 \quad (7)$$

> ComprobacionDos := eval(subs(y(x) = rhs(SolGral), Ecua))

$$ComprobacionDos := 0 = 0 \quad (8)$$

> restart
> EcuaCarac := (m - (2 + 3 I))2 · (m - (2 - 3 I))2 = 0

$$EcuaCarac := (m - 2 - 3 I)^2 (m - 2 + 3 I)^2 = 0 \quad (9)$$

> EcuaDos := expand(EcuaCarac)

$$EcuaDos := m^4 - 8 m^3 + 42 m^2 - 104 m + 169 = 0 \quad (10)$$

> EcuaEcua := y''' - 8 y'' + 42 y' - 104 y + 169 y = 0

$$\begin{aligned} EcuaEcua &:= \frac{d^4}{dx^4} y(x) - 8 \left( \frac{d^3}{dx^3} y(x) \right) + 42 \left( \frac{d^2}{dx^2} y(x) \right) - 104 \left( \frac{d}{dx} y(x) \right) + 169 y(x) \\ &= 0 \end{aligned} \quad (11)$$

> Sol := dsolve(EcuaEcua)

$$Sol := y(x) = _C1 e^{2x} \sin(3x) + _C2 e^{2x} \cos(3x) + _C3 e^{2x} \sin(3x)x + _C4 e^{2x} \cos(3x)x \quad (12)$$


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