

$$y'' + 4y' + 8y = e^{2x}(\sin(2x) + \cos(2x))$$

$$(D^2 + 4D + 8)y = 0 \quad Q = e^{2x}\cos(2x) + e^{2x}\sin(2x)$$

$$m^2 + 4m + 8 = 0$$

$$m = \frac{-4 \pm \sqrt{4^2 - 4(8)}}{2}$$

$$m = -2 \pm \sqrt{\frac{4^2 - 4(8)}{4}}$$

$$m = -2 \pm \sqrt{4 - 8}$$

$$m = -2 \pm \sqrt{-4}$$

$$m = -2 \pm 2i \quad \text{CASE III}$$

$$y_h = C_1 e^{-2x} \cos(2x) + C_2 e^{-2x} \sin(2x)$$

$$(D^2 + 4D + 8)y = e^{2x} \cos(2x) + e^{2x} \sin(2x)$$

$$(D^2 + 4D + 8)(D^2 - 4D + 8)y = 0$$

$$y_{nh} = C_1 e^{-2x} \cos(2x) + C_2 e^{-2x} \sin(2x) + A e^{2x} \cos(2x) + B e^{2x} \sin(2x)$$

$$y_p = A e^{2x} \cos(2x) + B e^{2x} \sin(2x)$$

$$\begin{array}{rcl} 16A + 16B = 1 & 16A = 1 - 16\left(\frac{1}{16}\right) \\ -16A + 16B = 1 & 16A = 1 - \frac{16}{16} \Rightarrow 0 \end{array}$$

$$32B = 2$$

$$B = \frac{1}{16}$$

$$A = 0$$

$$y'''+4y''+4y = x \sin(\sqrt{2}x)$$

$$(D^4 + 4D^2 + 4)y = x \sin(\sqrt{2}x)$$

$$m^4 + 4m^2 + 4 = 0$$

$$(m^2 + 2)^2 = 0$$

$$m_1 = \sqrt{2}, m_2 = -\sqrt{2}, m_3 = \sqrt{2}, m_4 = -\sqrt{2}$$

$$\underline{y_h = C_1 \cos(\sqrt{2}x) + C_2 \sin(\sqrt{2}x) + C_3 x \cos(\sqrt{2}x) + C_4 x \sin(\sqrt{2}x)}$$

$$(D^4 + 4D^2 + 4) \cdot (D^4 + 4D^2 + 4)y = 0$$

$$(D^4 + 4D^2 + 4)^2 y = 0$$

$$y = C_1 \cos(\sqrt{2}x) + C_2 \sin(\sqrt{2}x) + C_3 x \cos(\sqrt{2}x) + C_4 x \sin(\sqrt{2}x) +$$

$$+ A x^2 \cos(\sqrt{2}x) + B x^2 \sin(\sqrt{2}x) + D x^3 \cos(\sqrt{2}x) + E x^3 \sin(\sqrt{2}x)$$