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> restart
> Auno := A + D = 1; Ados := -6·A + B - 9·D + E = -11; Atres := 13·A - 3·B + C + 27·D - 9
   ·E = 36; Acuatro := -29·A + 4·B - 27·D + 27·E = -59; Acinco := 36·A - 12·B + 4·C
   - 27·E = 108
      Auno := A + D = 1
      Ados := -6 A + B - 9 D + E = -11
      Atres := 13 A - 3 B + C + 27 D - 9 E = 36
      Acuatro := -29 A + 4 B - 27 D + 27 E = -59
      Acinco := 36 A - 12 B + 4 C - 27 E = 108
(1)

> with(linalg) :
> Para := solve( {Auno, Ados, Atres, Acuatro, Acinco} )
      Para :=  $\left\{ A = \frac{936}{1121}, B = -\frac{4450}{1121}, C = \frac{4443}{1121}, D = \frac{185}{1121}, E = -\frac{600}{1121} \right\}$ 
(2)

> restart
> Ecua := diff(y(t), t$2) - 6·diff(y(t), t) + 9·y(t) = 3·exp(3·t) + 5·cos(2·t)
      Ecua :=  $\frac{d^2}{dt^2} y(t) - 6 \left( \frac{d}{dt} y(t) \right) + 9 y(t) = 3 e^{3t} + 5 \cos(2t)$ 
(3)

> CondIni := y(0) = 1, D(y)(0) = -2 plot(
      CondIni := y(0) = 1, D(y)(0) = -2
(4)

> with(inttrans) :
> EcuaTL := subs(CondIni, laplace(Ecua, t, s))
      EcuaTL :=  $s^2 \text{laplace}(y(t), t, s) + 8 - s - 6 s \text{laplace}(y(t), t, s) + 9 \text{laplace}(y(t), t, s) = \frac{3}{s-3}$ 
      +  $\frac{5 s}{s^2 + 4}$ 
(5)

> SolTL := simplify(isolate(EcuaTL, laplace(y(t), t, s)))
      SolTL :=  $\text{laplace}(y(t), t, s) = \frac{s^4 - 11 s^3 + 36 s^2 - 59 s + 108}{(s-3) (s^2 + 4) (s^2 - 6 s + 9)}$ 
(6)

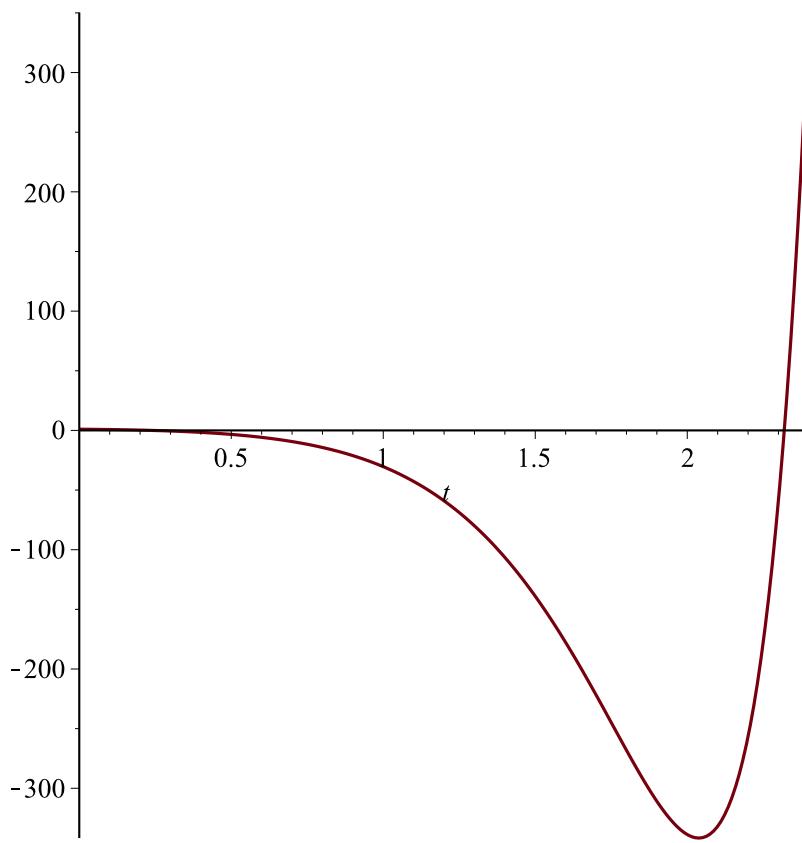
> SolPart := invlaplace(SolTL, s, t)
      SolPart :=  $y(t) = \frac{25}{169} \cos(2t) - \frac{60}{169} \sin(2t) + \frac{1}{338} e^{3t} (507 t^2 - 1300 t + 288)$ 
(7)

> CondIni := y(0) = simplify(subs(t=0, rhs(SolPart)))
      CondIni := y(0) = 1
(8)

> CondIniDer := D(y)(0) = simplify(subs(t=0, rhs(diff(SolPart, t))))
      CondIniDer := D(y)(0) = -2
(9)

> plot(rhs(SolPart), t=0 .. 2.4)

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> restart

> $\text{EcuaSist} := \text{diff}(x[1](t), t) = 2 \cdot x[1](t) + 3 \cdot x[2](t) + 4 \cdot t^2, \text{diff}(x[2](t), t) = x[1](t) + 4 \cdot x[2](t) + 2 \cdot \exp(3 \cdot t) : \text{EcuaSist}[1]; \text{EcuaSist}[2]$

$$\frac{d}{dt} x_1(t) = 2 x_1(t) + 3 x_2(t) + 4 t^2$$

$$\frac{d}{dt} x_2(t) = x_1(t) + 4 x_2(t) + 2 e^{3t} \quad (10)$$

> $\text{Ecua} := \text{diff}(x[2](t), t\$2) - 6 \cdot \text{diff}(x[2](t), t) + 5 \cdot x[2](t) = 4 \cdot t^2 + 2 \cdot \exp(3 \cdot t)$

$$\text{Ecua} := \frac{d^2}{dt^2} x_2(t) - 6 \left(\frac{d}{dt} x_2(t) \right) + 5 x_2(t) = 4 t^2 + 2 e^{3t} \quad (11)$$

> $\text{VarUno} := x[1](t) = \text{diff}(x[2](t), t) - 4 \cdot x[2](t) - 2 \cdot \exp(3 \cdot t)$

$$\text{VarUno} := x_1(t) = \frac{d}{dt} x_2(t) - 4 x_2(t) - 2 e^{3t} \quad (12)$$

> $\text{SolGral}[2] := \text{dsolve}(\text{Ecua})$

$$\text{SolGral}_2 := x_2(t) = e^t \text{C2} + e^{5t} \text{CI} - \frac{1}{2} e^{3t} + \frac{4}{5} t^2 + \frac{48}{25} t + \frac{248}{125} \quad (13)$$

> $\text{SolGral}[1] := \text{eval}(\text{subs}(x[2](t) = \text{rhs}(\text{SolGral}[2]), \text{VarUno}))$

$$SolGral_1 := x_1(t) = -3 e^t C2 + e^{5t} CI - \frac{3}{2} e^{3t} - \frac{152}{25} t - \frac{752}{125} - \frac{16}{5} t^2 \quad (14)$$

> $SolGral[2]$

$$x_2(t) = e^t C2 + e^{5t} CI - \frac{1}{2} e^{3t} + \frac{4}{5} t^2 + \frac{48}{25} t + \frac{248}{125} \quad (15)$$

> $EcuaSist[1]; EcuaSist[2]$

$$\begin{aligned} \frac{d}{dt} x_1(t) &= 2 x_1(t) + 3 x_2(t) + 4 t^2 \\ \frac{d}{dt} x_2(t) &= x_1(t) + 4 x_2(t) + 2 e^{3t} \end{aligned} \quad (16)$$

> $Comprobar := simplify(eval(subs(x[1](t) = rhs(SolGral[1]), x[2](t) = rhs(SolGral[2])), lhs(EcuaSist[1]) - rhs(EcuaSist[1]) = 0))$

$$Comprobar := 0 = 0 \quad (17)$$

> $ComprobarDos := simplify(eval(subs(x[1](t) = rhs(SolGral[1]), x[2](t) = rhs(SolGral[2])), lhs(EcuaSist[2]) - rhs(EcuaSist[2]) = 0))$

$$ComprobarDos := 0 = 0 \quad (18)$$

> $with(linalg) :$

> $AA := array([[2, 3], [1, 4]])$

$$AA := \begin{bmatrix} 2 & 3 \\ 1 & 4 \end{bmatrix} \quad (19)$$

> $MatExp := exponential(AA, t)$

$$MatExp := \begin{bmatrix} \frac{3}{4} e^t + \frac{1}{4} e^{5t} & \frac{3}{4} e^{5t} - \frac{3}{4} e^t \\ \frac{1}{4} e^{5t} - \frac{1}{4} e^t & \frac{1}{4} e^t + \frac{3}{4} e^{5t} \end{bmatrix} \quad (20)$$

> $Identidad := map(rcurry(eval, t=0'), MatExp)$

$$Identidad := \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} \quad (21)$$

>