

TEMA 3b SISTEMAS DE E.C.D.F. ORD. LINEALES

$$\begin{aligned} \textcircled{1} \quad \frac{dx_1}{dt} &= 2x_1 + 3x_2 & \frac{d}{dt}\bar{x} &= A\bar{x} \\ \textcircled{2} \quad \frac{dx_2}{dt} &= x_1 + 4x_2 & S(z) &\in \text{DO}(1) \text{ LccH.} \end{aligned}$$

De ②

$$x_1 = \frac{dx_2}{dt} - 4x_2 \quad \frac{d}{dt}\bar{x} = A\bar{x} + b(t) \quad \text{X/H.}$$

$$\frac{d}{dt} \left(\frac{dx_1}{dt} \right) = \frac{d^2 x_2}{dt^2} - 4 \frac{dx_2}{dt}$$

Sust. ①

$$\frac{d^2 x_2}{dt^2} - 4 \frac{dx_2}{dt} = 2 \left(\frac{dx_2}{dt} - 4x_2 \right) + 3x_2$$

$$\frac{d^2 x_2}{dt^2} - 4 \frac{dx_2}{dt} - 2 \frac{dx_2}{dt} + 8x_2 - 3x_2 = 0$$

$$\frac{d^2 x_2}{dt^2} - 6 \frac{dx_2}{dt} + 5x_2 = 0 \quad \text{EDO}(z) \text{ LccH.}$$

$$(D^2 - 6D + 5)x_2 = 0$$

$$(D-1)(D-5)x_2 = 0$$

$$x_2(t) = C_1 e^t + C_2 e^{5t}$$

$$\frac{dx_2}{dt} = C_1 e^t + 5C_2 e^{5t}$$

$$x_1(t) = (C_1 e^t + 5C_2 e^{5t}) - 4(C_1 e^t + C_2 e^{5t})$$

$$x_1(t) = -3C_1 e^t + C_2 e^{5t}$$

$$x_2(t) = C_1 e^t + C_2 e^{5t}$$

$$Sg - S(z) \in \text{DO}(1) \text{ LccH.}$$

$$\begin{aligned} \frac{dx_1}{dt} &= 2x_1(t) + 3x_2(t) \\ \frac{dx_2}{dt} &= x_1(t) + 4x_2(t) \end{aligned}$$

$$\frac{d^3 y(t)}{dt^3} + 2 \frac{d^2 y(t)}{dt^2} - 4 \frac{dy}{dt} - 6y = 0$$

EDO (3) LCC H.

$$y(t) \Rightarrow y_1(t)$$

$$\frac{dy(t)}{dt} \Rightarrow y_1'(t) = y_2(t)$$

$$\frac{d^2 y(t)}{dt^2} \Rightarrow y_2'(t) = y_3(t)$$

$$\frac{d^3 y(t)}{dt^3} = y_3'(t)$$

$$y_1'(t) = y_2(t)$$

$$y_2'(t) = y_3(t)$$

$$y_3'(t) = 6y_1(t) + 4y_2(t) - 2y_3(t)$$

S(3) EDO(1) LCC H.

$$\begin{aligned}\frac{dx_1(t)}{dt} &= 2x_1 + 3x_2 \\ \frac{dx_2(t)}{dt} &= x_1 + 4x_2\end{aligned}\quad \bar{x} = \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} \quad \frac{d\bar{x}}{dt} = \begin{bmatrix} \frac{dx_1}{dt} \\ \frac{dx_2}{dt} \end{bmatrix}$$

$$\frac{d}{dt} \begin{bmatrix} x_1(t) \\ x_2(t) \end{bmatrix} = \begin{bmatrix} 2 & 3 \\ 1 & 4 \end{bmatrix} \begin{bmatrix} x_1(t) \\ x_2(t) \end{bmatrix} \quad e^{At}$$

$$\frac{d}{dt} \bar{x} = A \bar{x}$$

$$\bar{x} = \begin{bmatrix} e^{At} \end{bmatrix} \bar{x}(0) \quad \bar{x}(0) = \begin{bmatrix} c_1 \\ c_2 \end{bmatrix}$$

$$e^{at}$$

$$\frac{d}{dt} e^{at} = a e^{at}$$

$$e^{a(0)} = 1$$

$$e^{a(-t)} = \frac{1}{e^a}$$

$$(e^{at})(e^{a-t}) = 1$$

$$e^{At}$$

$$\frac{d}{dt} e^{At} = A \times e^{At}$$

$$e^{A(0)} = I$$

$$e^{A(-t)} = e^{-A(t)}$$

$$e^{A(-t)} \times e^{At} = I$$