

Teorema de Existencia y Unicidad
de la transformada de Laplace
Dada una $f(t)$ existirá transf. Lapl.
cuando cumpla los sig. requisitos

a) sea de orden exponencial

b) sea seccionalmente continua

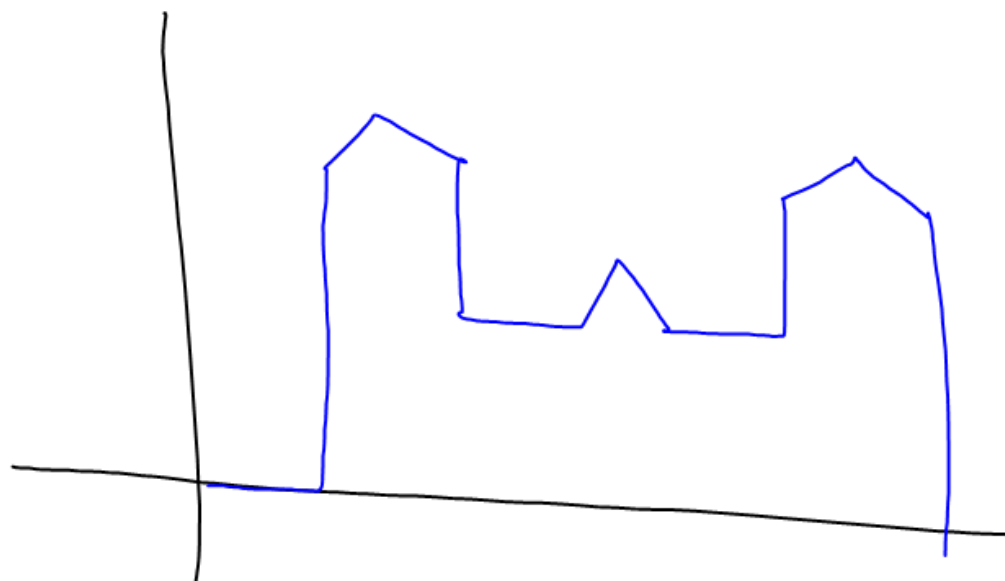
Sea de orden exponencial:

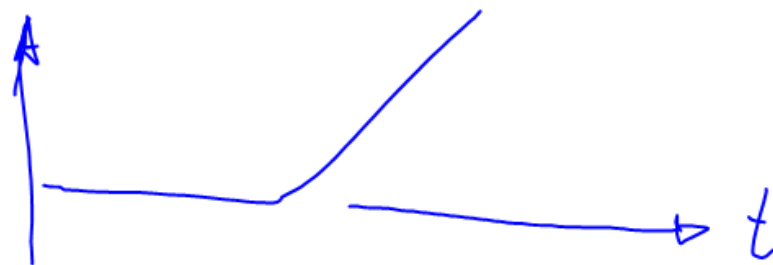
$$|f(t)| \leq M e^{at} \quad M, a \in \mathbb{R}$$

$$e^{5t} \quad \underbrace{e^{5t^2} \quad \dots \quad e^{5t^n}}_{n > 1}$$



$$L \frac{dI}{dt} + RI = 117 \cos(60t) u(t - a)$$







$$r(t-a) = \begin{cases} 0; & t < a \\ (t-a)u(t-a) & t \geq a \end{cases}$$



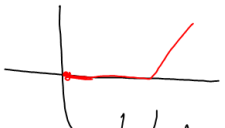
$$\delta(t-a) \begin{cases} 0; & t \neq a \\ \int_{-\infty}^{\infty} \delta(t-a) dt = 1 \end{cases}$$

$$\mathcal{L}\{f'(t)\} = s\mathcal{L}\{f(t)\} - f(0)$$

$$\mathcal{L}\{u(t-a)\} = \frac{e^{-as}}{s}$$


$$\mathcal{L}\{(t-a)u(t-a)\} = \frac{e^{-as}}{s^2}$$


$$\mathcal{L}\left\{\frac{d}{dt}((t-a)u(t-a))\right\} = s\mathcal{L}\{(t-a)u(t-a)\} - (0)$$

$$= s\left(\frac{e^{-as}}{s^2}\right)$$


$$= \left(\frac{e^{-as}}{s}\right)$$

$$\mathcal{L}\left\{\frac{d}{dt}((t-a)u(t-a))\right\} = \mathcal{L}\{u(t-a)\}$$

$$\frac{d}{dt}((t-a)u(t-a)) = u(t-a)$$

$$\mathcal{L}\{\delta(t-a)\} = e^{-as}$$

$$\mathcal{L}\left\{\frac{d}{dt}u(t-a)\right\} = s\mathcal{L}\{u(t-a)\} - (0)$$

$$\mathcal{L}\left\{\frac{d}{dt}u(t-a)\right\} = s\left(\frac{e^{-as}}{s}\right)$$

$$\mathcal{L}\left\{\frac{d}{dt}u(t-a)\right\} = e^{-as}$$

$$\mathcal{L}\left\{\frac{d}{dt}u(t-a)\right\} = \mathcal{L}\{\delta(t-a)\}$$

$$\frac{d}{dt}u(t-a) = \delta(t-a)$$
