

```
> restart
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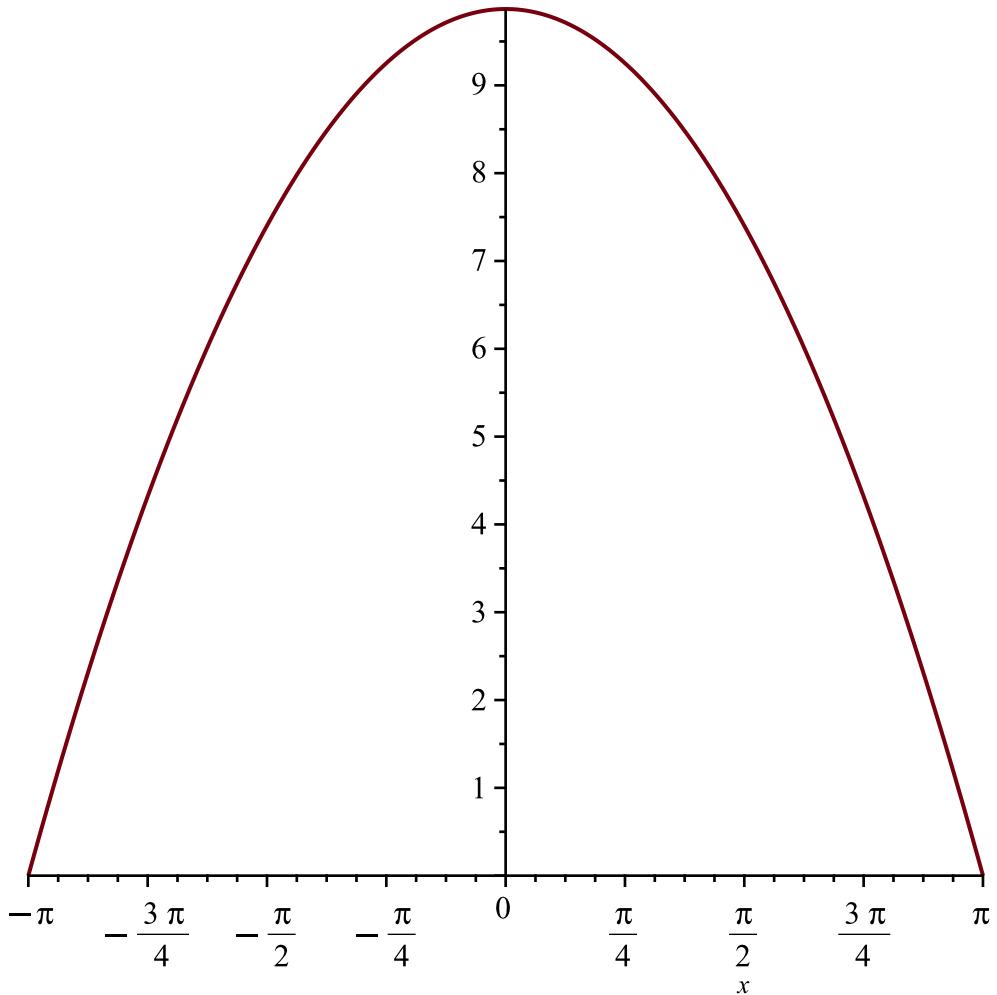
```
> f := π² - x²
```

$$f := \pi^2 - x^2 \quad (1)$$

```
> Intervalo := -Pi..Pi
```

$$\text{Intervalo} := -\pi..\pi \quad (2)$$

```
> plot(f, x = -Pi..Pi)
```



```
> L := Pi
```

$$L := \pi \quad (3)$$

```
> a[0] := 1/L · int(f, x = -L..L)
```

$$a_0 := \frac{4\pi^2}{3} \quad (4)$$

```
> a[n] := subs\left(\sin(n·\text{Pi}) = 0, \cos(n·\text{Pi}) = (-1)^n, \frac{1}{L} · \int(f · \cos\left(\frac{n·\text{Pi}}{L} · x\right), x = -L..L)\right)
```

$$a_n := -\frac{4(-1)^n}{n^2} \quad (5)$$

$$> b[n] := \text{subs}\left(\sin(n \cdot \text{Pi}) = 0, \cos(n \cdot \text{Pi}) = (-1)^n, \frac{1}{L} \cdot \text{int}\left(f \cdot \sin\left(\frac{n \cdot \text{Pi}}{L} \cdot x\right), x = -L..L\right)\right) \\ b_n := 0 \quad (6)$$

> restart

$$\begin{aligned} > f := & \text{Heaviside}(x + a) \cdot \exp(-a \cdot x) - \text{Heaviside}(x) \cdot \exp(-a \cdot x) + \text{Heaviside}(x) \cdot \exp(a \cdot x) \\ & - \text{Heaviside}(x - a) \cdot \exp(a \cdot x) \\ f := & \text{Heaviside}(x + a) e^{-ax} - \text{Heaviside}(x) e^{-ax} + \text{Heaviside}(x) e^{ax} - \text{Heaviside}(x - a) e^{ax} \end{aligned} \quad (7)$$

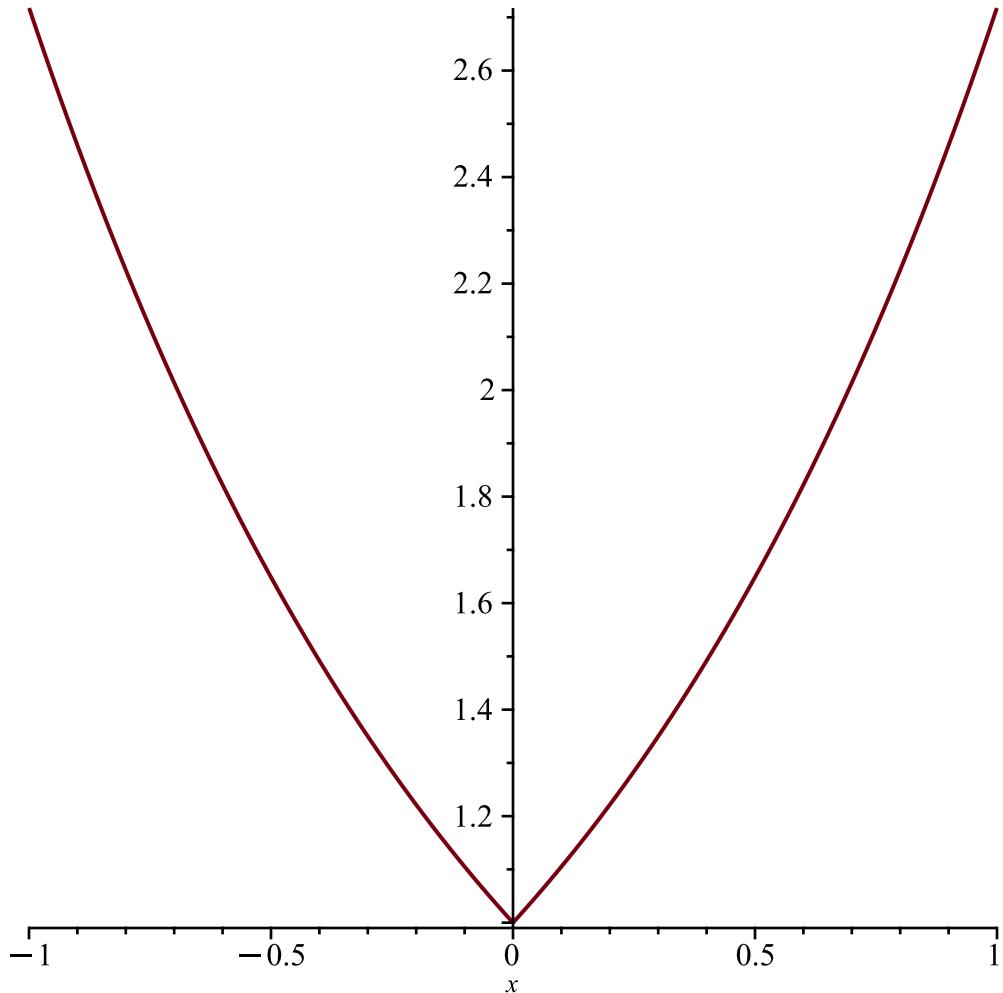
> Intervalo := -a .. 0

$$\text{Intervalo} := -a .. 0 \quad (8)$$

> h := subs(a = 1, f)

$$h := \text{Heaviside}(x + 1) e^{-x} - \text{Heaviside}(x) e^{-x} + \text{Heaviside}(x) e^x - \text{Heaviside}(x - 1) e^x \quad (9)$$

> plot(h, x = -1 .. 1)



> L := 1

$$L := 1 \quad (10)$$

> a[0] := $\frac{1}{L} \cdot \text{int}(h, x = -L..L)$

$$a_0 := 2e - 2 \quad (11)$$

$$> a[n] := \frac{1}{L} \cdot \text{int}\left(h \cdot \cos\left(\frac{n \cdot \text{Pi}}{L} \cdot x\right), x = -L..L\right)$$

$$a_n := \frac{-2 + 2 n \pi e \sin(n \pi) + 2 e \cos(n \pi)}{n^2 \pi^2 + 1} + \frac{-1 + n \pi e \sin(n \pi) + e \cos(n \pi)}{n^2 \pi^2 + 1}$$

$$+ \frac{-n \pi e \sin(n \pi) - e \cos(n \pi) + 1}{n^2 \pi^2 + 1}$$
(12)

$$> aa[0] := \text{subs}(a=1, a[0])$$

$$aa_0 := 2 e - 2$$
(13)

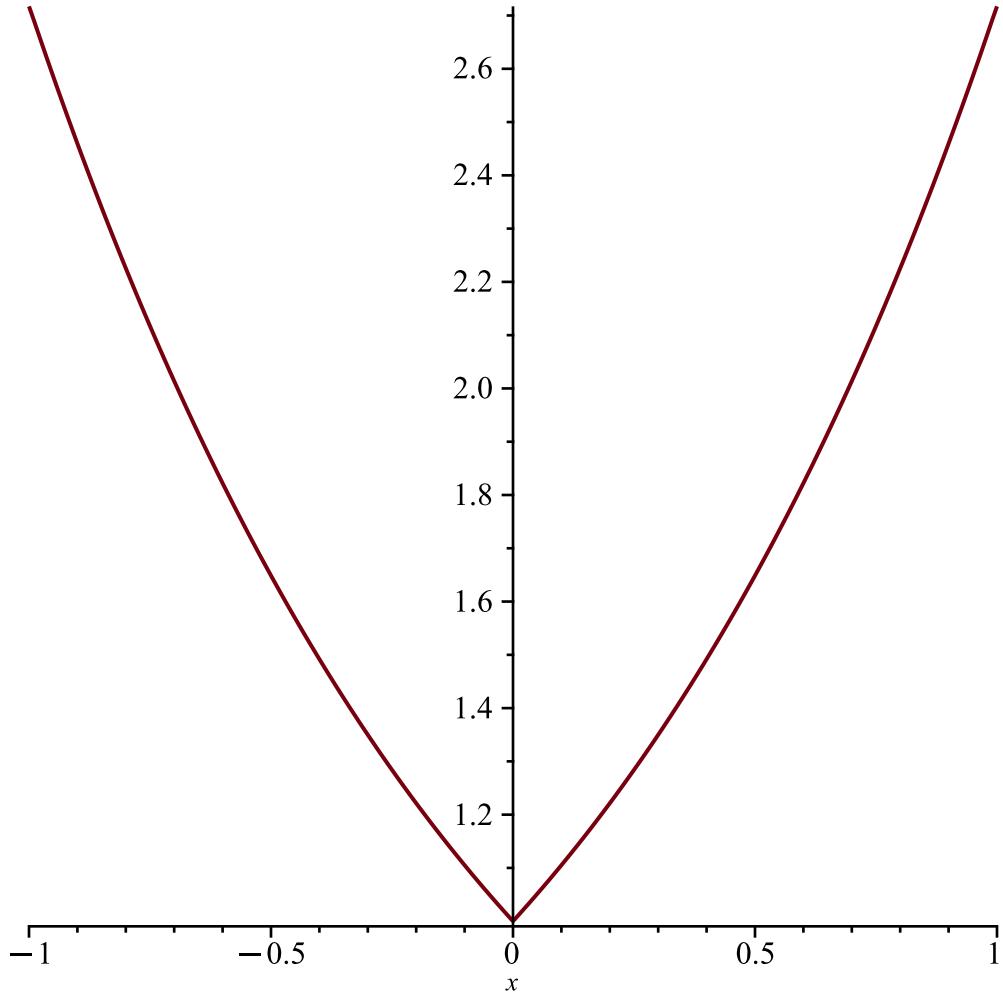
$$> aa[n] := \text{subs}(a=1, a[n])$$

$$aa_n := \frac{-2 + 2 n \pi e \sin(n \pi) + 2 e \cos(n \pi)}{n^2 \pi^2 + 1} + \frac{-1 + n \pi e \sin(n \pi) + e \cos(n \pi)}{n^2 \pi^2 + 1}$$

$$+ \frac{-n \pi e \sin(n \pi) - e \cos(n \pi) + 1}{n^2 \pi^2 + 1}$$
(14)

$$> STF500 := \frac{aa[0]}{2} + \text{sum}\left(aa[n] \cdot \cos\left(\frac{n \cdot \text{Pi}}{L} \cdot x\right), n = 1 .. 500\right) :$$

$$> \text{plot}(STF500, x = -L..L)$$



```

> restart
> Ecua := (3·x2 + 6·x·y(x)2) + (6·x2·y(x) + 4·y(x)3)·diff(y(x), x) = 0
      Ecua := 3 x2 + 6 x y(x)2 + (6 x2 y(x) + 4 y(x)3)  $\left( \frac{dy}{dx} \right) = 0$           (15)

> with(DEtools):
> odeadvisor(Ecua)
      [_exact, _rational]                                (16)

>
>
>

```