

> restart

> SolGral := y(x) = C₁·exp(2·x) + C₂·exp(-2·x) + C₃·exp(3·x) + C₄·exp(-3·x)

$$\text{SolGral} := y(x) = C_1 e^{2x} + C_2 e^{-2x} + C_3 e^{3x} + C_4 e^{-3x} \quad (1)$$

> Sistema := diff(SolGral, x), diff(SolGral, x\$2), diff(SolGral, x\$3), diff(SolGral, x\$4) :
Sistema₁; Sistema₂; Sistema₃; Sistema₄

$$\frac{d}{dx} y(x) = 2 C_1 e^{2x} - 2 C_2 e^{-2x} + 3 C_3 e^{3x} - 3 C_4 e^{-3x}$$

$$\frac{d^2}{dx^2} y(x) = 4 C_1 e^{2x} + 4 C_2 e^{-2x} + 9 C_3 e^{3x} + 9 C_4 e^{-3x}$$

$$\frac{d^3}{dx^3} y(x) = 8 C_1 e^{2x} - 8 C_2 e^{-2x} + 27 C_3 e^{3x} - 27 C_4 e^{-3x}$$

$$\frac{d^4}{dx^4} y(x) = 16 C_1 e^{2x} + 16 C_2 e^{-2x} + 81 C_3 e^{3x} + 81 C_4 e^{-3x} \quad (2)$$

> Parametro := solve({Sistema}, {C₁, C₂, C₃, C₄}) : Parametro₁; Parametro₂; Parametro₃;
Parametro₄;

$$C_1 = \frac{1}{40} \frac{18 \left(\frac{d}{dx} y(x) \right) - 2 \left(\frac{d^3}{dx^3} y(x) \right) + 9 \left(\frac{d^2}{dx^2} y(x) \right) - \left(\frac{d^4}{dx^4} y(x) \right)}{e^{2x}}$$

$$C_2 = -\frac{1}{40} \frac{18 \left(\frac{d}{dx} y(x) \right) - 2 \left(\frac{d^3}{dx^3} y(x) \right) - 9 \left(\frac{d^2}{dx^2} y(x) \right) + \frac{d^4}{dx^4} y(x)}{e^{-2x}}$$

$$C_3 = -\frac{1}{90} \frac{12 \left(\frac{d}{dx} y(x) \right) - 3 \left(\frac{d^3}{dx^3} y(x) \right) + 4 \left(\frac{d^2}{dx^2} y(x) \right) - \left(\frac{d^4}{dx^4} y(x) \right)}{e^{3x}}$$

$$C_4 = \frac{1}{90} \frac{12 \left(\frac{d}{dx} y(x) \right) - 3 \left(\frac{d^3}{dx^3} y(x) \right) - 4 \left(\frac{d^2}{dx^2} y(x) \right) + \frac{d^4}{dx^4} y(x)}{e^{-3x}} \quad (3)$$

> EcuacionInicial := subs(C₁ = rhs(Parametro₁), C₂ = rhs(Parametro₂), C₃ = rhs(Parametro₃), C₄ = rhs(Parametro₄), SolGral)

$$\text{EcuacionInicial} := y(x) = \frac{13}{36} \frac{d^2}{dx^2} y(x) - \frac{1}{36} \frac{d^4}{dx^4} y(x) \quad (4)$$

> EcuacionFinal := lhs(EcuacionInicial)·36 - rhs(EcuacionInicial)·36 = 0

$$\text{EcuacionFinal} := 36 y(x) - 13 \left(\frac{d^2}{dx^2} y(x) \right) + \frac{d^4}{dx^4} y(x) = 0 \quad (5)$$

> restart

> Ecuacion := y''' - 3 y'' + 3 y' - y = 0

$$\text{Ecuacion} := \frac{d^3}{dx^3} y(x) - 3 \left(\frac{d^2}{dx^2} y(x) \right) + 3 \left(\frac{d}{dx} y(x) \right) - y(x) = 0 \quad (6)$$

$$\begin{aligned} &> \text{Solucion} := \text{dsolve}(\text{Ecuacion}) \\ &\text{Solucion} := y(x) = _C1 e^x + _C2 e^x x + _C3 e^x x^2 \end{aligned} \quad (7)$$

restart

$$\begin{aligned} &> \text{Ecuacion} := y''' + 6 y'' + 21 y' + 26 y = 0 \\ &\text{Ecuacion} := \frac{d^3}{dx^3} y(x) + 6 \left(\frac{d^2}{dx^2} y(x) \right) + 21 \left(\frac{d}{dx} y(x) \right) + 26 y(x) = 0 \end{aligned} \quad (8)$$

$$\begin{aligned} &> \text{Solucion} := \text{dsolve}(\text{Ecuacion}) \\ &\text{Solucion} := y(x) = _C1 e^{-2x} + _C2 e^{-2x} \sin(3x) + _C3 e^{-2x} \cos(3x) \end{aligned} \quad (9)$$

restart

$$\begin{aligned} &> \text{EcuacCarac} := \text{expand}((m - 5I) \cdot 2 \cdot (m + 5I) \cdot 2) = 0 \\ &\text{EcuacCarac} := m^4 + 625 + 50 m^2 = 0 \end{aligned} \quad (10)$$

$$\begin{aligned} &> \text{Ecuacion} := y'''' + 50 y'' + 625 y = 0 \\ &\text{Ecuacion} := \frac{d^4}{dx^4} y(x) + 50 \left(\frac{d^2}{dx^2} y(x) \right) + 625 y(x) = 0 \end{aligned} \quad (11)$$

$$\begin{aligned} &> \text{SolucionGeneral} := \text{dsolve}(\text{Ecuacion}) \\ &\text{SolucionGeneral} := y(x) = _C1 \sin(5x) + _C2 \cos(5x) + _C3 \sin(5x) x + _C4 \cos(5x) x \end{aligned} \quad (12)$$