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# PROBLEMA DEL TIRO CON ARCO Y FLECHA (morada)

> EcuacionDinamica := Masa\_flecha · diff(s(t), t\$2) = Hooke · s(t)

$$EcuacionDinamica := Masa_{flecha} \left( \frac{d^2}{dt^2} s(t) \right) = Hooke s(t) \quad (1)$$

> Peso\_flecha :=  $\frac{20}{1000}$ ; gravedad :=  $\frac{98}{10}$ ; Hooke :=  $-\frac{\left(\frac{1922}{100}\right)}{\left(\frac{5}{10}\right)}$ ; Masa\_flecha :=  $\frac{Peso_{flecha}}{gravedad}$

$$Peso_{flecha} := \frac{1}{50}$$

$$gravedad := \frac{49}{5}$$

$$Hooke := -\frac{961}{25}$$

$$Masa_{flecha} := \frac{1}{490} \quad (2)$$

> EcuacionDinamica;

$$\frac{1}{490} \frac{d^2}{dt^2} s(t) = -\frac{961}{25} s(t) \quad (3)$$

> CondicionesDinamicas := s(0) = - $\frac{43}{100}$ , D(s)(0) = 0

$$CondicionesDinamicas := s(0) = -\frac{43}{100}, D(s)(0) = 0 \quad (4)$$

> Empuje\_flecha := dsolve({EcuacionDinamica, CondicionesDinamicas})

$$Empuje_{flecha} := s(t) = -\frac{43}{100} \cos\left(\frac{217}{5} \sqrt{10} t\right) \quad (5)$$

> Tiempo\_empuje := solve(rhs(Empuje\_flecha) = 0, t); evalf(%, 3)

$$Tiempo_{empuje} := \frac{1}{868} \pi \sqrt{10} \quad (6)$$

> Velocidad\_inicial := subs(t = Tiempo\_empuje, rhs(diff(Empuje\_flecha, t))); evalf(%, 3); evalf(%%, 3) · 3.6

$$Velocidad_{inicial} := \frac{9331}{500} \sin\left(\frac{1}{2} \pi\right) \sqrt{10} \quad (7)$$

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# PROBLEMA TIRO PARABÓLICO

> Velocidad\_inicial

$$\frac{9331}{500} \sqrt{10} \quad (8)$$

$$\begin{aligned}
&> \text{Ecuacion}_{vertical} := \text{diff}(y(t), t\$2) = -\text{gravedad}; \text{Ecuacion}_{horizontal} := \text{diff}(x(t), t) \\
&\quad = \text{Velocidad}_{inicial} \cdot \cos\left(\frac{\text{Pi}}{4}\right) \\
&\quad \text{Ecuacion}_{vertical} := \frac{d^2}{dt^2} y(t) = -\frac{49}{5} \\
&\quad \text{Ecuacion}_{horizontal} := \frac{d}{dt} x(t) = \frac{9331}{1000} \sqrt{10} \sqrt{2}
\end{aligned} \tag{9}$$

$$\begin{aligned}
&> \text{Condiciones}_{verticales} := y(0) = \frac{21}{10}, D(y)(0) = \text{Velocidad}_{inicial} \cdot \sin\left(\frac{\text{Pi}}{4}\right); \text{Condicion}_{horizontal} \\
&\quad := x(0) = 5 \\
&\quad \text{Condiciones}_{verticales} := y(0) = \frac{21}{10}, D(y)(0) = \frac{9331}{1000} \sqrt{10} \sqrt{2} \\
&\quad \text{Condicion}_{horizontal} := x(0) = 5
\end{aligned} \tag{10}$$

$$\begin{aligned}
&> \text{Recorrido}_{vertical} := \text{dsolve}(\{\text{Ecuacion}_{vertical}, \text{Condiciones}_{verticales}\}); \text{Recorrido}_{horizontal} \\
&\quad := \text{dsolve}(\{\text{Ecuacion}_{horizontal}, \text{Condicion}_{horizontal}\}) \\
&\quad \text{Recorrido}_{vertical} := y(t) = -\frac{49}{10} t^2 + \frac{9331}{1000} \sqrt{10} \sqrt{2} t + \frac{21}{10} \\
&\quad \text{Recorrido}_{horizontal} := x(t) = \frac{9331}{500} \sqrt{5} t + 5
\end{aligned} \tag{11}$$

$$\begin{aligned}
&> \text{TiempoVuelo} := \text{solve}(\text{rhs}(\text{Recorrido}_{vertical}) = 0, t); \text{evalf}(\%, 3) \\
&\quad \text{TiempoVuelo} := \frac{1333}{700} \sqrt{5} - \frac{1}{700} \sqrt{9094445}, \frac{1333}{700} \sqrt{5} + \frac{1}{700} \sqrt{9094445} \\
&\quad \quad -0.04, 8.56
\end{aligned} \tag{12}$$

$$\begin{aligned}
&> \text{DistanciaMaxima} := \text{subs}(t = \text{TiempoVuelo}_2, \text{rhs}(\text{Recorrido}_{horizontal})); \text{evalf}(\%, 3) \\
&\quad \text{DistanciaMaxima} := \frac{9331}{500} \sqrt{5} \left( \frac{1333}{700} \sqrt{5} + \frac{1}{700} \sqrt{9094445} \right) + 5 \\
&\quad \quad 364.
\end{aligned} \tag{13}$$

$$\begin{aligned}
&> \text{TiempoAlturaMaxima} := \text{solve}(\text{rhs}(\text{diff}(\text{Recorrido}_{vertical}, t)) = 0, t); \text{evalf}(\%, 3) \\
&\quad \text{TiempoAlturaMaxima} := \frac{1333}{1400} \sqrt{10} \sqrt{2} \\
&\quad \quad 4.25
\end{aligned} \tag{14}$$

$$\begin{aligned}
&> \text{AlturaMaxima} := \text{subs}(t = \text{TiempoAlturaMaxima}, \text{rhs}(\text{Recorrido}_{vertical})); \text{evalf}(\%, 3) \\
&\quad \text{AlturaMaxima} := \frac{1818889}{20000} \\
&\quad \quad 90.9
\end{aligned} \tag{15}$$

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