

$$\frac{d}{dt} \begin{bmatrix} x_1(t) \\ x_2(t) \end{bmatrix} = \begin{bmatrix} 1 & 1 \\ -1 & 1 \end{bmatrix} \begin{bmatrix} x_1(t) \\ x_2(t) \end{bmatrix} + \begin{bmatrix} 2e^{3t} + \cos(2t) \\ t^2 + 4t \end{bmatrix}$$

$\bar{x}(0) = \begin{bmatrix} 5 \\ -5 \end{bmatrix}$

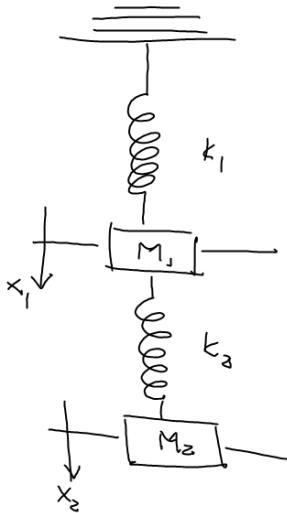
$$\frac{d}{dt} \bar{x} = A \bar{x} + b(t) \quad S(z) \rightarrow 0 \quad LCCNH$$

$$\bar{x} = e^{At} \bar{x}(0) + \int_0^t e^{A(t-z)} b(z) dz$$

$e^{At} \cdot \bar{x}(0)$  |  $t=0$  =  $x_{\text{zero}}$        $\int_0^t e^{A(t-z)} b(z) dz$  |  $t=0$  =  $[0]$

$$\frac{d}{dt} \bar{x}(t) = A \bar{x}(t) + b(t) \quad \bar{x}(a)$$

$$\bar{x}(t) = e^{A(t-a)} \cdot \bar{x}(a) + \int_a^t e^{A(t-z)} b(z) dz.$$



$$M_1 \frac{d^2x_1(t)}{dt^2} = \sum_{i=1}^2 F_i \\ = -k_1 x_1 + k_2 (x_2 - x_1)$$

$$M_2 \frac{d^2x_2(t)}{dt^2} = \sum_{j=1}^2 F_j \\ = -k_2 (x_2 - x_1)$$

$$\frac{d^2x_1(t)}{dt^2} = -\frac{k_1}{M_1} x_1 + \frac{k_2}{M_1} (x_2 - x_1) \quad \frac{dx_1}{dt} = x_3$$

$$\frac{d^2x_2(t)}{dt^2} = -\frac{k_2}{M_2} (x_2 - x_1) \quad \frac{dx_2}{dt} = x_4$$

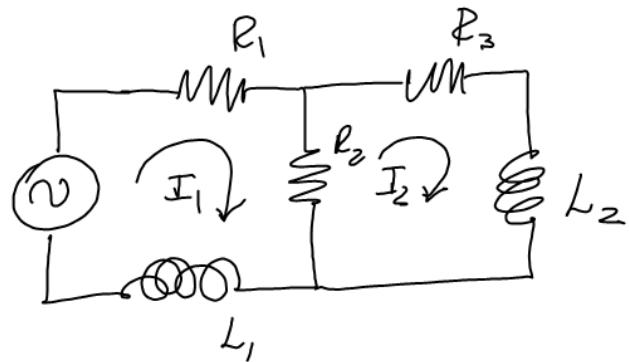
$$\frac{dx_3}{dt} = x_3$$

$$\frac{dx_4}{dt} = x_4$$

$$\frac{dx_3}{dt} = \left( -\frac{k_1}{M_1} - \frac{k_2}{M_1} \right) x_1 + \frac{k_2}{M_1} x_2$$

$$\frac{dx_4}{dt} = \frac{k_2}{M_2} x_1 - \frac{k_2}{M_2} x_2$$

$$\frac{d}{dt} \begin{bmatrix} x_1(t) \\ x_2(t) \\ x_3(t) \\ x_4(t) \end{bmatrix} = \begin{bmatrix} 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \\ -\left(\frac{k_1}{M_1} + \frac{k_2}{M_1}\right) & \frac{k_2}{M_1} & 0 & 0 \\ \frac{k_2}{M_2} & -\frac{k_2}{M_2} & 0 & 0 \end{bmatrix} \begin{bmatrix} x_1(t) \\ x_2(t) \\ x_3(t) \\ x_4(t) \end{bmatrix}$$



$$R_1 I_1 + R_2 (I_1 - I_2) + L_1 \frac{dI_1}{dt} = 120 \operatorname{sen}(60\pi t)$$

$$\underline{R_3 (I_2 - I_1) + R_2 I_2 + L_2 \frac{dI_2}{dt} = 0}$$

$$L_1 \frac{dI_1}{dt} = -(R_1 + R_2) I_1 + R_2 I_2 + 120 \operatorname{sen}(60\pi t)$$

$$L_2 \frac{dI_2}{dt} = +R_2 I_1 - (R_3 + R_2) I_2$$

$$\frac{dI_1}{dt} = -\frac{(R_1 + R_2)}{L_1} I_1 + \frac{R_2}{L_1} I_2 + 120 \operatorname{sen}(60\pi t)$$

$$\frac{dI_2}{dt} = \frac{R_2}{L_2} I_1 - \frac{(R_3 + R_2)}{L_2} I_2$$

$$\frac{d}{dt} \begin{bmatrix} I_1(t) \\ I_2(t) \end{bmatrix} = \begin{bmatrix} -\frac{(R_1 + R_2)}{L_1} & \frac{R_2}{L_1} \\ \frac{R_2}{L_2} & -\frac{(R_3 + R_2)}{L_2} \end{bmatrix} \begin{bmatrix} I_1(t) \\ I_2(t) \end{bmatrix} + \begin{bmatrix} 120 \operatorname{sen}(60\pi t) \\ 0 \end{bmatrix}$$

