

LUNES 12 - S. J106

LUNES 19 - TERCER PARCIAL  
J205

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Método: CUANDO TODOS LOS TÉRMINOS  
DE LA EDAD TIENEN EL  
MISMO ORDEN.

Método de Variables Separables.  
- General, de prueba y error.

$$\frac{\partial^2 z(x,y)}{\partial x^2} + 5 \frac{\partial^2 z(x,y)}{\partial y^2} = 0$$

H<sub>0</sub>:

$$z(x,y) = F(x) \cdot G(y)$$

$$\frac{\partial z}{\partial x} = F'(x) \cdot G(y) \quad \frac{\partial z}{\partial y} = F(x) \cdot G'(y)$$

$$\frac{\partial^2 z}{\partial x^2} = F''(x) \cdot G(y)$$

$$F''(x)G(y) + 5 F(x)G'(y) = 0$$

$$F''(x)G(y) = -5 F(x)G'(y)$$

$$\frac{\cancel{F''(x)} \cancel{G(y)}}{\cancel{F(x)} \cancel{G(y)}} = -5 \frac{\cancel{F(x)} \cancel{G'(y)}}{\cancel{F(x)} \cancel{G(y)}}$$

$$\left\{ \begin{array}{l} \frac{F''(x)}{F(x)} = -5 \frac{G'(y)}{G(y)} \\ \boxed{\frac{F''(x)}{5F(x)} = -\frac{G'(y)}{G(y)}} \\ -\frac{F''(x)}{5F(x)} = \frac{G'(y)}{G(y)} \\ -\frac{F''(x)}{F(x)} = \frac{5G'(y)}{G(y)} \end{array} \right\} \begin{array}{l} \text{La hipótesis} \\ \text{es} \\ \text{válida} \end{array}$$

$$H_1: z(x,y) = F(x) + G(y) \quad \times$$

$$H_2: z(x,y) = \frac{F(x)}{G(y)} \quad z(x,y) = \frac{G(y)}{F(x)}$$

$$H_3: z(x,y) = F(x)^y \quad G(y)^x$$

$$H_4: z(x,y) = F(x) \cdot G(y)$$

$$\frac{F''(x)}{5F(x)} = - \frac{G'(y)}{G(y)}$$

$$\frac{F''(x)}{5F(x)} = \alpha \quad - \frac{G'(y)}{G(y)} = \alpha$$

$$\alpha = 0$$

$$\alpha > 0$$

$$\alpha < 0$$

$$\frac{F''(x)}{5F(x)} = 0 \quad F(x) \neq 0 \quad F''(x) = 0$$

$$F'(x) = k_1$$

$$F(x) = k_1 x + k_2$$

$$- \frac{G'(y)}{G(y)} = 0$$

$$G(y) \neq 0$$

$$G'(y) = 0$$

$$G(y) = C_1$$

$$Z(x, y) = (k_1 x + k_2) C_1$$

$$Z(x, y) = k_{10} x + k_{20}$$

$$\alpha > 0 \quad \alpha = k^2 \quad \forall k \neq 0 \in \mathbb{R}$$

$$\frac{F''(x)}{5F(x)} = k^2 \quad F''(x) = 5k^2 F(x)$$

$$m^2 - 5k^2 = 0$$

$$F''(x) - 5k^2 F(x) = 0$$

$$\pm \text{EDO}(z) \subset \mathbb{C} \text{ t.t.}$$

$$(m - \sqrt{5}k)(m + \sqrt{5}k) = 0$$

$$m_1 = \sqrt{5}k \quad m_2 = -\sqrt{5}k$$

$$F(x) = C_1 e^{\sqrt{5}kx} + C_2 e^{-\sqrt{5}kx}$$

$$-\frac{G'(y)}{G(y)} = k^2$$

$$G'(y) = -k^2 G(y) \quad \pm \text{EDO}(1) \subset \mathbb{C} \text{ t.t.}$$

$$G'(y) + k^2 G(y) = 0$$

$$G(y) = K_1 e^{-k^2 y}$$

$$Z(x, y) = (C_1 e^{\sqrt{5}kx} + C_2 e^{-\sqrt{5}kx}) (K_1 e^{-k^2 y})$$

$$= C_{10} e^{\sqrt{5}kx - k^2 y} + C_{20} e^{-\sqrt{5}kx - k^2 y}$$

$$Z(x, y) = C_{10} e^{(\sqrt{5}kx - k^2 y)} + C_{20} e^{-(\sqrt{5}kx + k^2 y)}$$

$$\alpha < 0 \quad \alpha = -k^2 \quad \forall k \neq 0 \in \mathbb{R}$$

$$\frac{F''(x)}{5F(x)} = -k^2 \quad F''(x) = -5k^2 F(x)$$

$$F''(x) + 5k^2 F(x) = 0 \quad \text{EDO(2)} \text{ L.O.C. 4.}$$

$$m^2 + 5k^2 = 0 \quad m_1 = -\sqrt{5}k i$$

$$m_2 = \sqrt{5}k i$$

$$F(x) = C_1 \cos(\sqrt{5}kx) + C_2 \operatorname{sen}(\sqrt{5}kx)$$

$$-\frac{g'(y)}{g(y)} = -k^2 \quad g(y) = K_1 e^{k^2 y}$$

$$Z(x, y) = C_{10} e^{k^2 y} \cos(\sqrt{5}kx) + C_{20} e^{k^2 y} \operatorname{sen}(\sqrt{5}kx)$$