

> restart

$$y = C_1 e^x + C_2 x e^x + C_3 e^x \cos(x)$$

> SolGral := $y(x) = C_1 \cdot \exp(x) + C_2 \cdot x \cdot 2 \cdot \exp(x) + C_3 \cdot \exp(x) \cdot \cos(x)$

$$SolGral := y(x) = C_1 e^x + C_2 x^2 e^x + C_3 e^x \cos(x) \quad (1)$$

> Sistema := diff(SolGral, x), diff(SolGral, x\$2), diff(SolGral, x\$3) : Sistema₁; Sistema₂;

Sistema₃

$$\frac{d}{dx} y(x) = C_1 e^x + 2 C_2 x e^x + C_2 x^2 e^x + C_3 e^x \cos(x) - C_3 e^x \sin(x)$$

$$\frac{d^2}{dx^2} y(x) = C_1 e^x + 2 C_2 e^x + 4 C_2 x e^x + C_2 x^2 e^x - 2 C_3 e^x \sin(x)$$

$$\frac{d^3}{dx^3} y(x) = C_1 e^x + 6 C_2 e^x + 6 C_2 x e^x + C_2 x^2 e^x - 2 C_3 e^x \sin(x) - 2 C_3 e^x \cos(x) \quad (2)$$

> Parametro := simplify(solve({Sistema}, {C₁, C₂, C₃})) : Parametro₁

$$\begin{aligned} C_1 &= \frac{1}{2} \frac{1}{2 \sin(x) + \sin(x) x - x \cos(x)} \left(\left(6 \left(\frac{d^2}{dx^2} y(x) \right) \cos(x) + 2 \sin(x) \left(\frac{d^3}{dx^3} y(x) \right) \right. \right. \\ &\quad - 6 \sin(x) \left(\frac{d^2}{dx^2} y(x) \right) - 2 \cos(x) \left(\frac{d^3}{dx^3} y(x) \right) - 4 \left(\frac{d}{dx} y(x) \right) \cos(x) \\ &\quad + 10 x \left(\frac{d^2}{dx^2} y(x) \right) \cos(x) - 2 x \sin(x) \left(\frac{d^2}{dx^2} y(x) \right) - 4 x \cos(x) \left(\frac{d^3}{dx^3} y(x) \right) \\ &\quad - 8 x \left(\frac{d}{dx} y(x) \right) \cos(x) + 3 x^2 \left(\frac{d^2}{dx^2} y(x) \right) \cos(x) - x^2 \sin(x) \left(\frac{d^3}{dx^3} y(x) \right) \\ &\quad + x^2 \sin(x) \left(\frac{d^2}{dx^2} y(x) \right) - x^2 \cos(x) \left(\frac{d^3}{dx^3} y(x) \right) - 2 x^2 \left(\frac{d}{dx} y(x) \right) \cos(x) \\ &\quad \left. \left. + 8 \sin(x) \left(\frac{d}{dx} y(x) \right) + 4 \sin(x) x \left(\frac{d}{dx} y(x) \right) \right) e^{-x} \right) \end{aligned} \quad (3)$$

> Ecuacion := simplify(subs(C₁=rhs(Parametro₁), C₂=rhs(Parametro₂), C₃=rhs(Parametro₃), SolGral))

$$\begin{aligned} Ecuacion &:= y(x) = -\frac{1}{2 \sin(x) + \sin(x) x - x \cos(x)} \left(-\sin(x) \left(\frac{d^3}{dx^3} y(x) \right) \right. \\ &\quad \left. + 3 \sin(x) \left(\frac{d^2}{dx^2} y(x) \right) - 3 x \left(\frac{d^2}{dx^2} y(x) \right) \cos(x) + x \sin(x) \left(\frac{d^2}{dx^2} y(x) \right) \right) \end{aligned} \quad (4)$$

$$+ x \cos(x) \left(\frac{d^3}{dx^3} y(x) \right) + 3 x \left(\frac{d}{dx} y(x) \right) \cos(x) - 2 \sin(x) x \left(\frac{d}{dx} y(x) \right)$$

$$- 4 \sin(x) \left(\frac{d}{dx} y(x) \right) \Bigg)$$

> *EcuacionFinal := simplify(lhs(Ecuacion) · (2 sin(x) + sin(x) x - x cos(x)) - rhs(Ecuacion) · (2 sin(x) + sin(x) x - x cos(x))) = 0*

$$\begin{aligned} EcuacionFinal := & 2 y(x) \sin(x) + y(x) \sin(x) x - y(x) x \cos(x) - \sin(x) \left(\frac{d^3}{dx^3} y(x) \right) \\ & + 3 \sin(x) \left(\frac{d^2}{dx^2} y(x) \right) - 3 x \left(\frac{d^2}{dx^2} y(x) \right) \cos(x) + x \sin(x) \left(\frac{d^2}{dx^2} y(x) \right) \\ & + x \cos(x) \left(\frac{d^3}{dx^3} y(x) \right) + 3 x \left(\frac{d}{dx} y(x) \right) \cos(x) - 2 \sin(x) x \left(\frac{d}{dx} y(x) \right) \\ & - 4 \sin(x) \left(\frac{d}{dx} y(x) \right) = 0 \end{aligned} \quad (5)$$

E.D.O.(3)L.c.v.H.

> *Solucion := dsolve(EcuacionFinal)*

$$Solucion := y(x) = e^x (-_C2 \cos(x) - 2_C3 x^2 + _C1) \quad (6)$$

> *restart*

$$\frac{d^2y}{dx^2} - 3 \frac{dy}{dx} + 2y = 8e^{3x} + 36e^{4x}$$

> *Ecuacion := y'' - 3 y' + 2 y = 8 · exp(3 x) + 36 · exp(4 x)*

$$Ecuacion := \frac{d^2}{dx^2} y(x) - 3 \left(\frac{d}{dx} y(x) \right) + 2 y(x) = 8 e^{3x} + 36 e^{4x} \quad (7)$$

> *Soluciongeneral := expand(dsolve(Ecuacion))*

$$Soluciongeneral := y(x) = 4 (e^x)^3 + 6 (e^x)^4 + (e^x)^2 _C1 + e^x _C2 \quad (8)$$

> *restart*

E.D.O.(2)L.cc.NH

> *Ecuacion := y'' + y' + y = 8 · exp(2 x) · sin(2 x)*

$$Ecuacion := \frac{d^2}{dx^2} y(x) + \frac{d}{dx} y(x) + y(x) = 8 e^{2x} \sin(2 x) \quad (9)$$

$$\frac{dy^2}{dx^2} + \frac{dy}{dx} + y = 8e^{2x} \sin(2x)$$

> EcuacionHomogena := lhs(Ecuacion) = 0

$$EcuacionHomogena := \frac{d^2}{dx^2} y(x) + \frac{d}{dx} y(x) + y(x) = 0 \quad (10)$$

> Q := rhs(Ecuacion)

$$Q := 8 e^{2x} \sin(2x) \quad (11)$$

> EcuacionCaracteristica := m··2 + m + 1 = 0

$$EcuacionCaracteristica := m^2 + m + 1 = 0 \quad (12)$$

> Raiz := solve(EcuacionCaracteristica)

$$Raiz := -\frac{1}{2} + \frac{1}{2} i\sqrt{3}, -\frac{1}{2} - \frac{1}{2} i\sqrt{3} \quad (13)$$

> SolUno := y(x) = exp(Re(Raiz1)·x) · cos(Im(Raiz1)·x)

$$SolUno := y(x) = e^{-\frac{1}{2}x} \cos\left(\frac{1}{2}\sqrt{3}x\right) \quad (14)$$

> SolDos := y(x) = exp(Re(Raiz1)·x) · sin(Im(Raiz1)·x)

$$SolDos := y(x) = e^{-\frac{1}{2}x} \sin\left(\frac{1}{2}\sqrt{3}x\right) \quad (15)$$

> with(linalg);

[BlockDiagonal, GramSchmidt, JordanBlock, LUdecomp, QRdecomp, Wronskian, addcol,

addrow, adj, adjoint, angle, augment, backsub, band, basis, bezout, blockmatrix, charmat,

charpoly, cholesky, col, coldim, colspace, colspan, companion, concat, cond, copyinto,

crossprod, curl, definite, delcols, delrows, det, diag, diverge, dotprod, eigenvals,

eigenvalues, eigenvectors, eigenvects, entermatrix, equal, exponential, extend, ffgausselim,

fibonacci, forwardsub, frobenius, gausselim, gaussjord, geneqns, genmatrix, grad,

hadamard, hermite, hessian, hilbert, htranspose, ihermite, indexfunc, innerprod, intbasis,

inverse, ismith, issimilar, iszero, jacobian, jordan, kernel, laplacian, leastsqr, linsolve,

matadd, matrix, minor, minpoly, mulcol, mulrow, multiply, norm, normalize, nullspace,

orthog, permanent, pivot, potential, randmatrix, randvector, rank, ratform, row, rowdim,

rowspace, rowspan, rref, scalarmul, singularvals, smith, stackmatrix, submatrix, subvector,

sumbasis, swapcol, swaprow, sylvester, toeplitz, trace, transpose, vandermonde, vecpotent,

vectdim, vector, wronskian]

> WW := wronskian([rhs(SolUno), rhs(SolDos)], x)

$$WW := \left[\left[e^{-\frac{1}{2}x} \cos\left(\frac{1}{2}\sqrt{3}x\right), e^{-\frac{1}{2}x} \sin\left(\frac{1}{2}\sqrt{3}x\right) \right] \right], \quad (17)$$

$$\left[-\frac{1}{2} e^{-\frac{1}{2}x} \cos\left(\frac{1}{2}\sqrt{3}x\right) - \frac{1}{2} e^{-\frac{1}{2}x} \sin\left(\frac{1}{2}\sqrt{3}x\right)\sqrt{3}, -\frac{1}{2} e^{-\frac{1}{2}x} \sin\left(\frac{1}{2}\sqrt{3}x\right) + \frac{1}{2} e^{-\frac{1}{2}x} \cos\left(\frac{1}{2}\sqrt{3}x\right)\sqrt{3} \right]$$

> $BB := array([0, Q])$

$$BB := \begin{bmatrix} 0 & 8 e^{2x} \sin(2x) \end{bmatrix} \quad (18)$$

> $SOL := simplify(linsolve(WW, BB)) : A prima := SOL_1; B prima := SOL_2$

$$\begin{aligned} A prima &:= -\frac{16}{3} \sqrt{3} e^{\frac{5}{2}x} \sin\left(\frac{1}{2}\sqrt{3}x\right) \sin(2x) \\ B prima &:= \frac{16}{3} \sqrt{3} e^{\frac{5}{2}x} \cos\left(\frac{1}{2}\sqrt{3}x\right) \sin(2x) \end{aligned} \quad (19)$$

> $A := int(A prima, x) + C_1 : B := int(B prima, x) + C_2 :$

> $SolucionNoHomogenea := y(x) = expand(simplify(A \cdot rhs(SolUno) + B \cdot rhs(SolDos)))$

$$\begin{aligned} SolucionNoHomogenea &:= y(x) = \frac{48}{109} e^{-\frac{1}{2}x} \cos\left(\frac{1}{2}\sqrt{3}x\right)^2 e^{\frac{5}{2}x} \sin(x) \cos(x) \\ &\quad + \frac{48}{109} e^{-\frac{1}{2}x} \sin\left(\frac{1}{2}\sqrt{3}x\right)^2 e^{\frac{5}{2}x} \sin(x) \cos(x) \\ &\quad - \frac{160}{109} e^{-\frac{1}{2}x} \cos\left(\frac{1}{2}\sqrt{3}x\right)^2 e^{\frac{5}{2}x} \cos(x)^2 - \frac{160}{109} e^{-\frac{1}{2}x} \sin\left(\frac{1}{2}\sqrt{3}x\right)^2 e^{\frac{5}{2}x} \cos(x)^2 \\ &\quad + \frac{80}{109} e^{-\frac{1}{2}x} \cos\left(\frac{1}{2}\sqrt{3}x\right)^2 e^{\frac{5}{2}x} + \frac{80}{109} e^{-\frac{1}{2}x} \sin\left(\frac{1}{2}\sqrt{3}x\right)^2 e^{\frac{5}{2}x} \\ &\quad + e^{-\frac{1}{2}x} \cos\left(\frac{1}{2}\sqrt{3}x\right) C_1 + e^{-\frac{1}{2}x} \sin\left(\frac{1}{2}\sqrt{3}x\right) C_2 \end{aligned} \quad (20)$$

> $SolGral := dsolve(Ecuacion)$

$$\begin{aligned} SolGral &:= y(x) = e^{-\frac{1}{2}x} \sin\left(\frac{1}{2}\sqrt{3}x\right) - C_2 + e^{-\frac{1}{2}x} \cos\left(\frac{1}{2}\sqrt{3}x\right) - C_1 - \frac{8}{109} (10 \cos(2x) \\ &\quad - 3 \sin(2x)) e^{2x} \end{aligned} \quad (21)$$

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