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> restart
> Ecuacion := x·4·log(x) - 2·x·y(x)·3 + 3·x·2·y(x)·2·y'(x) = 0
      Ecuacion := x4 ln(x) - 2 x y(x)3 + 3 x2 y(x)2 (  $\frac{d}{dx}$  y(x) ) = 0 (1)

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> with(DEtools)
[AreSimilar, DENormal, DEplot, DEplot3d, DEplot_polygon, DFactor, DFactorLCLM, (2)
 DFactorsols, Dchangevar, FunctionDecomposition, GCRD, Gosper, Heunsols,
 Homomorphisms, IVPsol, IsHyperexponential, LCLM, MeijerGsols,
 MultiplicativeDecomposition, ODEInvariants, PDEchangecoords, PolynomialNormalForm,
 RationalCanonicalForm, ReduceHyperexp, RiemannPsols, Xchange, Xcommutator, Xgauge,
 Zeilberger, abelsol, adjoint, autonomous, bernoullisol, buildsol, buildsym, canoni, caseplot,
 casesplit, checkrank, chinisol, clairautsol, constcoeffsols, convertAlg, convertsys,
 dalembertsol, dcoeffs, de2diffop, dfieldplot, diff_table, diffop2de, dperiodic_sols, dpolyform,
 dsubs, eigenring, endomorphism_charpoly, equinv, eta_k, eulersols, exactsol, expsols,
 exterior_power, firint, firtest, formal_sol, gen_exp, generate_ic, genhomosol, gensys,
 hamilton_eqs, hypergeomsols, hyperode, indicialeq, infgen, initialdata, integrate_sols,
 intfactor, invariants, kovacicols, leftdivision, liesol, line_int, linearsol, matrixDE,
 matrix_riccati, maxdimsystems, moser_reduce, muchange, mult, mutest, newton_polygon,
 normalG2, ode_int_y, ode_y1, odeadvisor, odepde, parametricsol, particularsol,
 phaseportrait, poincare, polysols, power_equivalent, rational_equivalent, ratsols, redode,
 reduceOrder, reduce_order, regular_parts, regularsp, remove_RootOf, riccati_system,
 riccatisol, rifread, rifsimp, rightdivision, rtaylor, separablesol, singularities, solve_group,
 super_reduce, symgen, symmetric_power, symmetric_product, symtest, transinv, translate,
 untranslate, varparam, zoom]

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> odeadvisor(Ecuacion)
      [_Bernoulli] (3)

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> FactInt := intfactor(Ecuacion)
      FactInt :=  $\frac{1}{x^4}$  (4)

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> M := x·4·log(x) - 2·x·y·3
      M := x4 ln(x) - 2 x y3 (5)

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> N := 3·x·2·y·2
      N := 3 y2 x2 (6)

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> MM := expand(FactInt·M); NN := FactInt·N
      MM := ln(x) -  $\frac{2 y^3}{x^3}$ 
      NN :=  $\frac{3 y^2}{x^2}$  (7)

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> Comprobacion := diff(MM, y) - diff(NN, x) = 0
      Comprobacion := 0 = 0 (8)

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$$\begin{aligned} &> \text{EcuacionDos} := \ln(x) - \frac{2y(x)^3}{x^3} + \frac{3y(x)^2}{x^2} \cdot \text{diff}(y(x), x) = 0 \\ &\quad \text{EcuacionDos} := \ln(x) - \frac{2y(x)^3}{x^3} + \frac{3y(x)^2 \left(\frac{d}{dx} y(x) \right)}{x^2} = 0 \end{aligned} \quad (9)$$

$$\begin{aligned} &> \text{odeadvisor}(\text{EcuacionDos}) \\ &\quad \quad \quad [\text{_exact}, \text{_Bernoulli}] \end{aligned} \quad (10)$$

$$\begin{aligned} &> \text{IntMMx} := \text{int}(\text{MM}, x) \\ &\quad \quad \quad \text{IntMMx} := x \ln(x) - x + \frac{y^3}{x^2} \end{aligned} \quad (11)$$

$$\begin{aligned} &> \text{SolucionGeneral} := \text{IntMMx} + \text{int}((\text{NN} - \text{diff}(\text{IntMMx}, y)), y) = C_1 \\ &\quad \quad \quad \text{SolucionGeneral} := x \ln(x) - x + \frac{y^3}{x^2} = C_1 \end{aligned} \quad (12)$$

$$\begin{aligned} &> \text{SolCero} := \text{isolate}(\text{SolucionGeneral}, y \cdot 3) \\ &\quad \quad \quad \text{SolCero} := y^3 = (C_1 - x \ln(x) + x) x^2 \end{aligned} \quad (13)$$

> restart

$$\begin{aligned} &> \text{Ecuacion} := 3 \cdot \exp(x) \cdot \tan(y) + (2 - \exp(x)) \cdot \sec(y) \cdot 2 \cdot y' = 0 \\ &\quad \quad \quad \text{Ecuacion} := 3 e^x \tan(y(x)) + (2 - e^x) \sec(y(x))^2 \left(\frac{d}{dx} y(x) \right) = 0 \end{aligned} \quad (14)$$

> with(DEtools):

$$\begin{aligned} &> \text{odeadvisor}(\text{Ecuacion}) \\ &\quad \quad \quad [\text{_separable}] \end{aligned} \quad (15)$$

$$\begin{aligned} &> M := 3 \cdot \exp(x) \cdot \tan(y); N := (2 - \exp(x)) \cdot \sec(y) \cdot 2; \\ &\quad \quad \quad M := 3 e^x \tan(y) \\ &\quad \quad \quad N := (2 - e^x) \sec(y)^2 \end{aligned} \quad (16)$$

$$\begin{aligned} &> P := 3 \cdot \exp(x); Q := \tan(y); R := (2 - \exp(x)); S := \sec(y) \cdot 2 \\ &\quad \quad \quad P := 3 e^x \\ &\quad \quad \quad Q := \tan(y) \\ &\quad \quad \quad R := 2 - e^x \\ &\quad \quad \quad S := \sec(y)^2 \end{aligned} \quad (17)$$

$$\begin{aligned} &> \text{SolucionGeneral} := \text{int}\left(\frac{P}{R}, x\right) + \text{int}\left(\frac{S}{Q}, y\right) = \log(C_1) \\ &\quad \quad \quad \text{SolucionGeneral} := -3 \ln(2 - e^x) + \ln(\tan(y)) = \ln(C_1) \end{aligned} \quad (18)$$

$$\begin{aligned} &> \text{Solucion} := \text{isolate}(\text{SolucionGeneral}, y) \\ &\quad \quad \quad \text{Solucion} := y = -\arctan\left(-8 C_1 + 12 C_1 e^x - 6 C_1 (e^x)^2 + C_1 (e^x)^3\right) \end{aligned} \quad (19)$$

> restart