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> restart
> Ecuacion := 2·diff(z(x, y), x$2, y) - 2·diff(z(x, y), x, y) = z(x, y)
      Ecuacion := 2  $\left( \frac{\partial^3}{\partial y \partial x^2} z(x, y) \right) - 2 \left( \frac{\partial^2}{\partial y \partial x} z(x, y) \right) = z(x, y) \quad (1)$ 

> EcuacionDos := eval(subs(z(x, y) = F(x) · G(y), Ecuacion))
      EcuacionDos := 2  $\left( \frac{d^2}{dx^2} F(x) \right) \left( \frac{d}{dy} G(y) \right) - 2 \left( \frac{d}{dx} F(x) \right) \left( \frac{d}{dy} G(y) \right) = F(x) G(y) \quad (2)$ 

> EcuacionTres := simplify  $\left( \frac{lhs(EcuacionDos)}{2 \cdot F(x) \cdot diff(G(y), y)} \right) = simplify \left( \frac{rhs(EcuacionDos)}{2 \cdot F(x) \cdot diff(G(y), y)} \right)$ 
      EcuacionTres := 
$$\frac{\frac{d^2}{dx^2} F(x) - \left( \frac{d}{dx} F(x) \right)}{F(x)} = \frac{1}{2} \frac{\frac{G(y)}{d}{dy}}{G(y)} \quad (3)$$


> EcuacionX := lhs(EcuacionTres) = -1
      EcuacionX := 
$$\frac{\frac{d^2}{dx^2} F(x) - \left( \frac{d}{dx} F(x) \right)}{F(x)} = -1 \quad (4)$$


> EcuacionY := rhs(EcuacionTres) = -1
      EcuacionY := 
$$\frac{1}{2} \frac{G(y)}{\frac{d}{dy} G(y)} = -1 \quad (5)$$


> SolucionX := dsolve(EcuacionX); SolucionY := dsolve(EcuacionY)
      SolucionX := F(x) =  $_C1 e^{\frac{1}{2}x} \sin\left(\frac{1}{2}\sqrt{3}x\right) + _C2 e^{\frac{1}{2}x} \cos\left(\frac{1}{2}\sqrt{3}x\right)$ 
      SolucionY := G(y) =  $_C1 e^{-\frac{1}{2}y} \quad (6)$ 

> Ecuacion
      
$$2 \left( \frac{\partial^3}{\partial y \partial x^2} z(x, y) \right) - 2 \left( \frac{\partial^2}{\partial y \partial x} z(x, y) \right) = z(x, y) \quad (7)$$


> SolucionGeneral := z(x, y) = rhs(SolucionX) · subs(_C1 = 1, rhs(SolucionY))
      SolucionGeneral := z(x, y) =  $\left( _C1 e^{\frac{1}{2}x} \sin\left(\frac{1}{2}\sqrt{3}x\right) + _C2 e^{\frac{1}{2}x} \cos\left(\frac{1}{2}\sqrt{3}x\right) \right) e^{-\frac{1}{2}y} \quad (8)$ 

> Comprobacion1 := simplify(eval(subs(z(x, y) = rhs(SolucionGeneral), lhs(Ecuacion) - rhs(Ecuacion) = 0)))
      Comprobacion1 := 0 = 0 \quad (9)
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