

TEM 9 1. :- EDO(1)NL

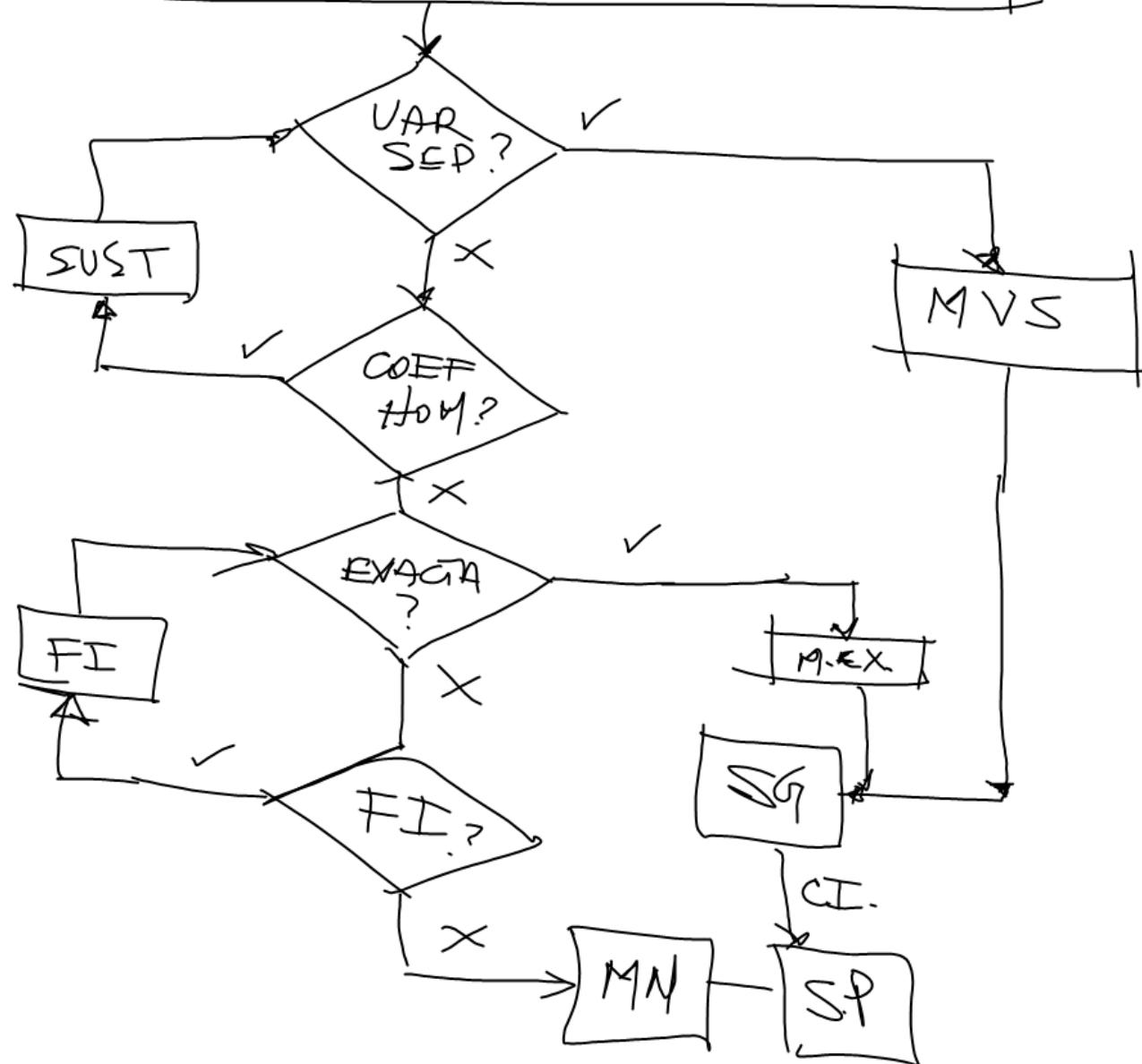
$$\frac{dy}{dx} = F(x, y)$$

$$\frac{dy}{dx} = - \frac{M(x, y)}{N(x, y)}$$

$$N \frac{dy}{dx} = -M$$

$$\boxed{M + N \frac{dy}{dx} = 0}$$
EDO(1)NL

$$\left(h(x, y) + N(x, y) \frac{dy}{dx} \right) = 0$$



$M \leq T D O$ VARIABLES SEP.

$$e^y(1+x^2) \frac{dy}{dx} - 2x(1+e^y) = 0$$

$$\curvearrowleft M(x, y) + N(x, y) \frac{dy}{dx} = 0$$

$$\rightarrow P(x)Q(y) + R(x)S(y) \frac{dy}{dx} = 0$$

$$\begin{aligned} P(x) &= -2x & R(x) &= 1+x^2 \\ Q(y) &= 1+e^y & S(y) &= e^y \end{aligned}$$

$$P(x)Q(y) + R(x)S(y) \frac{dy}{dx} = 0$$

$$\frac{P(x)Q(y)}{Q(y)R(x)} + \frac{R(x)S(y)}{Q(y)R(x)} \cdot \frac{dy}{dx} = 0$$

$$\frac{P(x)}{R(x)} + \frac{S(y)}{Q(y)} \cdot \frac{dy}{dx} = 0$$

$$\frac{P(x)}{R(x)} dx + \frac{S(y)}{Q(y)} dy = 0$$

(SG)

$$EDO(1) NL \int \frac{P(x)}{R(x)} dx + \int \frac{S(y)}{Q(y)} dy = C_1$$

$$\begin{array}{ll} P(x) = -2x & R(x) = (1+x^2) \\ Q(y) = (1+e^y) & S(y) = e^y \end{array}$$

$$\int \frac{-2x}{(1+x^2)} dx + \int \frac{e^y}{(1+e^y)} dy = C_1$$

$$-2 \ln(1+x^2) + \ln(1+e^y) = C_1$$

log

$$\ln \left(\frac{1+e^y}{1+x^2} \right) = C_1 \rightarrow e^{C_1}.$$

$$\frac{1+e^y}{1+x^2} = C_{10}$$


(SG)

$$1+e^y = C_{10} (1+x^2)$$