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> restart
> Ecua := y'' + 6 y' + 9 y = 8·exp(−3 x) − 6·cos(2 x)
      Ecua :=  $\frac{d^2}{dx^2} y(x) + 6 \frac{d}{dx} y(x) + 9 y(x) = 8 e^{-3x} - 6 \cos(2x)$  (1)
> SolaGral := dsolve(Ecua)
      SolaGral :=  $y(x) = e^{-3x} c_2 + e^{-3x} x c_1 + 4 e^{-3x} x^2 - \frac{30 \cos(2x)}{169} - \frac{72 \sin(2x)}{169}$  (2)
> restart
> Ecua := y'' + 6 y' + 9 y = 8·exp(−3 x) − 6·cos(2 x)
      Ecua :=  $\frac{d^2}{dx^2} y(x) + 6 \frac{d}{dx} y(x) + 9 y(x) = 8 e^{-3x} - 6 \cos(2x)$  (3)
> EcuaHom := lhs(Ecua) = 0
      EcuaHom :=  $\frac{d^2}{dx^2} y(x) + 6 \frac{d}{dx} y(x) + 9 y(x) = 0$  (4)
> Q := rhs(Ecua)
      Q :=  $8 e^{-3x} - 6 \cos(2x)$  (5)
> EcuaCarac := m^2 + 6 m + 9 = 0
      EcuaCarac :=  $m^2 + 6 m + 9 = 0$  (6)
> Raiz := solve(EcuaCarac)
      Raiz :=  $-3, -3$  (7)
> yy[1] := exp(Raiz[1]·x); yy[2] := x·exp(Raiz[1]·x)
      yy1 :=  $e^{-3x}$ 
      yy2 :=  $x e^{-3x}$  (8)
> SolGralHom := y(x) = _C1·yy[1] + _C2·yy[2]
      SolGralHom :=  $y(x) = _C1 e^{-3x} + _C2 x e^{-3x}$  (9)
> SolGralNoHom := y(x) = A·yy[1] + B·yy[2]
      SolGralNoHom :=  $y(x) = A e^{-3x} + B x e^{-3x}$  (10)
> with(linalg) :
> WW := wronskian([yy[1], yy[2]], x)
      WW :=  $\begin{bmatrix} e^{-3x} & x e^{-3x} \\ -3 e^{-3x} & e^{-3x} - 3 x e^{-3x} \end{bmatrix}$  (11)
> BB := array([0, Q])
      BB :=  $\begin{bmatrix} 0 & 8 e^{-3x} - 6 \cos(2x) \end{bmatrix}$  (12)
> Parametro := simplify(linsolve(WW, BB))
      Parametro :=  $\begin{bmatrix} 6 x e^{3x} \cos(2x) - 8 x & -6 \cos(2x) e^{3x} + 8 \end{bmatrix}$  (13)
> Aprima := Parametro[1]
      Aprima :=  $6 x e^{3x} \cos(2x) - 8 x$  (14)

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$$\begin{aligned} &> Bprima := Parametro[2] \\ &Bprima := -6 \cos(2x) e^{3x} + 8 \end{aligned} \quad (15)$$

$$\begin{aligned} &> A := \text{int}(Aprima, x) + _C1 \\ &A := -4x^2 + 6 \left(\frac{3x}{13} - \frac{5}{169} \right) e^{3x} \cos(2x) - 6 \left(-\frac{2x}{13} + \frac{12}{169} \right) e^{3x} \sin(2x) + _C1 \end{aligned} \quad (16)$$

$$\begin{aligned} &> B := \text{int}(Bprima, x) + _C2 \\ &B := 8x - \frac{18 \cos(2x) e^{3x}}{13} - \frac{12 \sin(2x) e^{3x}}{13} + _C2 \end{aligned} \quad (17)$$

$$\begin{aligned} &> SolGralNoHomFinal := \text{simplify}(SolGralNoHom) \\ &SolGralNoHomFinal := y(x) = e^{-3x} (x_C2 + 4x^2 + _C1) - \frac{30 \cos(2x)}{169} - \frac{72 \sin(2x)}{169} \end{aligned} \quad (18)$$

> restart

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