

SERIE 3 SEMESTRE 2024-2

> restart

> restart

1a)

> $f := \text{Heaviside}(t - 2) \cdot t \cdot \exp(-2t)$

$$f := \text{Heaviside}(t - 2) t e^{-2t} \quad (1)$$

> with(inttrans) :

> $F := \text{laplace}(f, t, s)$

$$F := \frac{(5 + 2s) e^{-4-2s}}{(2 + s)^2} \quad (2)$$

>

1b)

> $G := \frac{s \cdot \exp(-s)}{s^2 + s - 2}$

$$G := \frac{s e^{-s}}{s^2 + s - 2} \quad (3)$$

> $g := \text{invlaplace}(G, s, t)$

$$g := \frac{\text{Heaviside}(t - 1) (2 e^{-2t+2} + e^{t-1})}{3} \quad (4)$$

> restart

2) Obtenga la solución del sistema

> $\text{Sistema} := 2 \cdot \text{diff}(x(t), t) + \text{diff}(y(t), t) - 2 \cdot x(t) = 1, \text{diff}(x(t), t) + \text{diff}(y(t), t) - 3 \cdot x(t) - 3 \cdot y(t) = 2 : \text{Sistema}[1]; \text{Sistema}[2]$

$$2 \frac{d}{dt} x(t) + \frac{d}{dt} y(t) - 2 x(t) = 1$$

$$\frac{d}{dt} x(t) + \frac{d}{dt} y(t) - 3 x(t) - 3 y(t) = 2 \quad (5)$$

> $\text{CondIni} := x(0) = 0, y(0) = 0$

$$\text{CondIni} := x(0) = 0, y(0) = 0 \quad (6)$$

> $\text{Sist} := \text{Sistema}[1] - \text{Sistema}[2], -\text{Sistema}[1] + 2 \cdot \text{Sistema}[2] : \text{Sist}[1]; \text{Sist}[2]$

$$\frac{d}{dt} x(t) + x(t) + 3 y(t) = -1$$

$$\frac{d}{dt} y(t) - 4 x(t) - 6 y(t) = 3 \quad (7)$$

> $\text{SistDos} := \text{lhs}(\text{Sist}[1]) - (x(t) + 3 y(t)) = \text{rhs}(\text{Sist}[1]) - (x(t) + 3 y(t)), \text{lhs}(\text{Sist}[2]) - (-4 x(t) - 6 y(t)) = \text{rhs}(\text{Sist}[2]) - (-4 x(t) - 6 y(t)) : \text{SistDos}[1]; \text{SistDos}[2]$

$$\frac{d}{dt} x(t) = -1 - x(t) - 3 y(t)$$

$$\frac{d}{dt} y(t) = 3 + 4 x(t) + 6 y(t) \quad (8)$$

$$\begin{aligned} > AA := \text{array}([[-1, -3], [4, 6]]) \\ AA &:= \begin{bmatrix} -1 & -3 \\ 4 & 6 \end{bmatrix} \end{aligned} \quad (9)$$

$$\begin{aligned} > BB := \text{array}([-1, 3]) \\ BB &:= [-1 \quad 3] \end{aligned} \quad (10)$$

$$\begin{aligned} > Xcero := \text{array}([0, 0]) \\ Xcero &:= [0 \quad 0] \end{aligned} \quad (11)$$

$$\begin{aligned} > \text{with}(\text{linalg}) : \\ > \text{MatExp} := \text{exponential}(AA, t) \\ \text{MatExp} &:= \begin{bmatrix} 4 e^{2t} - 3 e^{3t} & -3 e^{3t} + 3 e^{2t} \\ 4 e^{3t} - 4 e^{2t} & -3 e^{2t} + 4 e^{3t} \end{bmatrix} \end{aligned} \quad (12)$$

$$\begin{aligned} > \text{SolHom} := \text{evalm}(\text{MatExp} \&* Xcero) \\ \text{SolHom} &:= [0 \quad 0] \end{aligned} \quad (13)$$

$$\begin{aligned} > \text{MatExpTau} := \text{map}(\text{rcurry}(\text{eval}, t='t - \text{tau}'), \text{MatExp}) \\ \text{MatExpTau} &:= \begin{bmatrix} 4 e^{2t-2\tau} - 3 e^{3t-3\tau} & -3 e^{3t-3\tau} + 3 e^{2t-2\tau} \\ 4 e^{3t-3\tau} - 4 e^{2t-2\tau} & -3 e^{2t-2\tau} + 4 e^{3t-3\tau} \end{bmatrix} \end{aligned} \quad (14)$$

$$\begin{aligned} > \text{BBtau} := \text{map}(\text{rcurry}(\text{eval}, t='tau'), BB) \\ \text{BBtau} &:= [-1 \quad 3] \end{aligned} \quad (15)$$

$$\begin{aligned} > \text{ProdTau} := \text{evalm}(\text{MatExpTau} \&* \text{BBtau}) \\ \text{ProdTau} &:= [5 e^{2t-2\tau} - 6 e^{3t-3\tau} \quad 8 e^{3t-3\tau} - 5 e^{2t-2\tau}] \end{aligned} \quad (16)$$

$$\begin{aligned} > \text{SolNoHom} := \text{map}(\text{int}, \text{ProdTau}, \text{tau} = 0 .. t) \\ \text{SolNoHom} &:= \begin{bmatrix} -\frac{1}{2} + \frac{5 e^{2t}}{2} - 2 e^{3t} & -\frac{1}{6} - \frac{5 e^{2t}}{2} + \frac{8 e^{3t}}{3} \end{bmatrix} \end{aligned} \quad (17)$$

$$\begin{aligned} > \text{SolPartFinal} := \text{evalm}(\text{SolHom} + \text{SolNoHom}) : x(t) = \text{SolPartFinal}[1]; y(t) = \text{SolPartFinal}[2] \\ x(t) &= -\frac{1}{2} + \frac{5 e^{2t}}{2} - 2 e^{3t} \\ y(t) &= -\frac{1}{6} - \frac{5 e^{2t}}{2} + \frac{8 e^{3t}}{3} \end{aligned} \quad (18)$$

$$\begin{aligned} > \text{Sistema}[1]; \text{Sistema}[2] \\ 2 \frac{d}{dt} x(t) + \frac{d}{dt} y(t) - 2 x(t) &= 1 \\ \frac{d}{dt} x(t) + \frac{d}{dt} y(t) - 3 x(t) - 3 y(t) &= 2 \end{aligned} \quad (19)$$

$$\begin{aligned} > \text{ComprobacionUno} := \text{eval}(\text{subs}(x(t) = \text{SolPartFinal}[1], y(t) = \text{SolPartFinal}[2], \text{Sistema}[1])) \\ \text{ComprobacionUno} &:= 1 = 1 \end{aligned} \quad (20)$$

$$> \text{ComprobacionDos} := \text{eval}(\text{subs}(x(t) = \text{SolPartFinal}[1], y(t) = \text{SolPartFinal}[2], \text{Sistema}[2]))$$

$$\text{ComprobacionDos} := 2 = 2 \quad (21)$$

$$\begin{aligned} > \text{CondIniUno} := \text{simplify}(\text{subs}(t=0, x(t) = \text{SolPartFinal}[1])) \\ & \text{CondIniUno} := x(0) = 0 \end{aligned} \quad (22)$$

$$\begin{aligned} > \text{CondIniDos} := \text{simplify}(\text{subs}(t=0, y(t) = \text{SolPartFinal}[2])) \\ & \text{CondIniDos} := y(0) = 0 \end{aligned} \quad (23)$$

> restart

3)

$$\begin{aligned} > \text{Ecu} := \text{diff}(y(t), t^2) + 6 \cdot \text{diff}(y(t), t) + 5 \cdot y(t) = \text{Dirac}(t - 1) \cdot \exp(t) \\ & \text{Ecu} := \frac{d^2}{dt^2} y(t) + 6 \frac{d}{dt} y(t) + 5 y(t) = \text{Dirac}(t - 1) e^t \end{aligned} \quad (24)$$

$$\begin{aligned} > \text{CondIni} := y(0) = 0, D(y)(0) = 4 \\ & \text{CondIni} := y(0) = 0, D(y)(0) = 4 \end{aligned} \quad (25)$$

> with(inttrans) :

$$\begin{aligned} > \text{EcuTL} := \text{subs}(\text{CondIni}, \text{laplace}(\text{Ecu}, t, s)) \\ & \text{EcuTL} := s^2 \mathcal{L}(y(t), t, s) - 4 + 6s \mathcal{L}(y(t), t, s) + 5 \mathcal{L}(y(t), t, s) = e^{1-s} \end{aligned} \quad (26)$$

$$\begin{aligned} > \text{SolTL} := \text{isolate}(\text{EcuTL}, \text{laplace}(y(t), t, s)) \\ & \text{SolTL} := \mathcal{L}(y(t), t, s) = \frac{e^{1-s} + 4}{s^2 + 6s + 5} \end{aligned} \quad (27)$$

$$\begin{aligned} > \text{SolPart} := \text{invlaplace}(\text{SolTL}, s, t) \\ & \text{SolPart} := y(t) = \frac{\text{Heaviside}(t - 1) \sinh(2t - 2) e^{4-3t}}{2} + 2 e^{-3t} \sinh(2t) \end{aligned} \quad (28)$$

$$\begin{aligned} > \text{Comprobacion} := \text{simplify}(\text{eval}(\text{subs}(y(t) = \text{rhs}(\text{SolPart}), \text{Ecu}))) \\ & \text{Comprobacion} := e \text{Dirac}(t - 1) = e \text{Dirac}(t - 1) \end{aligned} \quad (29)$$

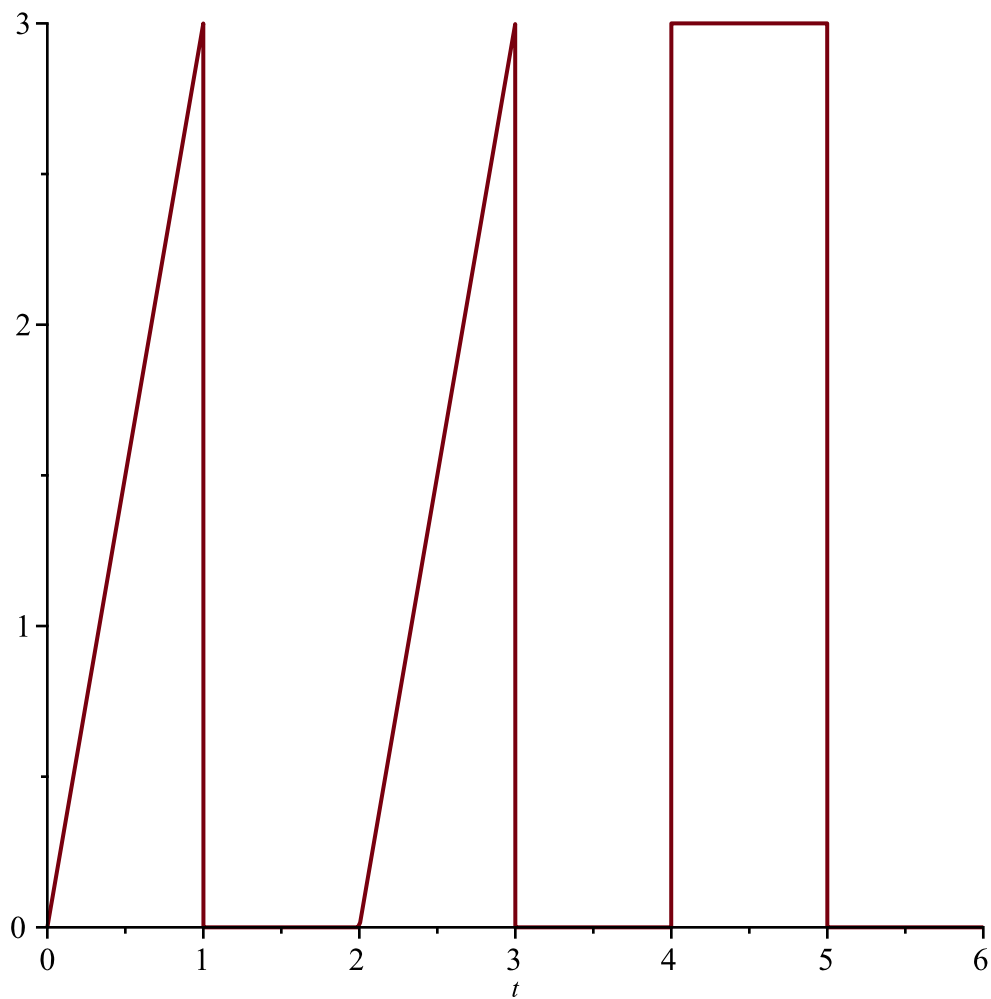
$$\begin{aligned} > \text{ComprobarDos} := y(0) = \text{simplify}(\text{subs}(t=0, \text{rhs}(\text{SolPart}))) \\ & \text{ComprobarDos} := y(0) = 0 \end{aligned} \quad (30)$$

$$\begin{aligned} > \text{ComprobarTres} := D(y)(0) = \text{simplify}(\text{subs}(t=0, \text{rhs}(\text{diff}(\text{SolPart}, t)))) \\ & \text{ComprobarTres} := D(y)(0) = 4 \end{aligned} \quad (31)$$

> restart

4)

$$\begin{aligned} > f := 3 \cdot t \cdot \text{Heaviside}(t) - 3 \cdot (t - 1) \cdot \text{Heaviside}(t - 1) - 3 \cdot \text{Heaviside}(t - 1) + 3 \cdot (t - 2) \\ & \cdot \text{Heaviside}(t - 2) - 3 \cdot (t - 3) \cdot \text{Heaviside}(t - 3) - 3 \cdot \text{Heaviside}(t - 3) + 3 \cdot \text{Heaviside}(t \\ & - 4) - 3 \cdot \text{Heaviside}(t - 5) : \text{plot}(f, t=0..6) \end{aligned}$$



> with(inttrans) :

> F := laplace(f, t, s)

$$F := \frac{3(1 - e^{-3s} + e^{-2s} - e^{-s})}{s^2} - \frac{3(e^{-s} + e^{-5s} - e^{-4s} + e^{-3s})}{s} \quad (32)$$

> restart

5)

> Ecua := diff(y(t), t\$2) - 2·diff(y(t), t) - 8·y(t) = 6·exp(-2 t)

$$Ecua := \frac{d^2}{dt^2} y(t) - 2 \frac{d}{dt} y(t) - 8 y(t) = 6 e^{-2t} \quad (33)$$

> CondIni := y(0) = 0, D(y)(0) = -7

$$CondIni := y(0) = 0, D(y)(0) = -7 \quad (34)$$

> with(inttrans) :

> EcuaTL := subs(CondIni, laplace(Ecua, t, s))

$$EcuaTL := s^2 \mathcal{L}(y(t), t, s) + 7 - 2s \mathcal{L}(y(t), t, s) - 8 \mathcal{L}(y(t), t, s) = \frac{6}{s+2} \quad (35)$$

> SolTL := isolate(EcuaTL, laplace(y(t), t, s))

(36)

$$\text{SolTL} := \mathcal{L}(y(t), t, s) = \frac{\frac{6}{s+2} - 7}{s^2 - 2s - 8} \quad (36)$$

> $\text{SolPart} := \text{invlaplace}(\text{SolTL}, s, t)$

$$\text{SolPart} := y(t) = -e^{4t} - e^{-2t}(t - 1) \quad (37)$$

>

5b) Convertir la ecuación a un sistema y resolverlo con matriz exponencial

> $\text{Ecua} := \text{diff}(y(t), t^2) - 2 \cdot \text{diff}(y(t), t) - 8 \cdot y(t) = 6 \cdot \exp(-2t)$

$$\text{Ecua} := \frac{d^2}{dt^2} y(t) - 2 \frac{d}{dt} y(t) - 8y(t) = 6e^{-2t} \quad (38)$$

> $\text{VarUno} := y(t) = y[1](t)$

$$\text{VarUno} := y(t) = y_1(t) \quad (39)$$

> $\text{Sist}[1] := \text{diff}(y[1](t), t) = y[2](t)$

$$\text{Sist}_1 := \frac{d}{dt} y_1(t) = y_2(t) \quad (40)$$

> $\text{Sist}[2] := \text{diff}(y[2](t), t) = 8y[1](t) + 2 \cdot y[2](t) + 6 \cdot \exp(-2t)$

$$\text{Sist}_2 := \frac{d}{dt} y_2(t) = 8y_1(t) + 2y_2(t) + 6e^{-2t} \quad (41)$$

> $\text{CondIni} := y[1](0) = 0, y[2](0) = -7$

$$\text{CondIni} := y_1(0) = 0, y_2(0) = -7 \quad (42)$$

> $\text{AA} := \text{array}([[0, 1], [8, 2]])$

$$\text{AA} := \begin{bmatrix} 0 & 1 \\ 8 & 2 \end{bmatrix} \quad (43)$$

> $\text{Xcero} := \text{array}([0, -7])$

$$\text{Xcero} := [0 \quad -7] \quad (44)$$

> $\text{BB} := \text{array}([0, 6 \cdot \exp(-2t)])$

$$\text{BB} := [0 \quad 6e^{-2t}] \quad (45)$$

> $\text{with}(\text{linalg}) :$

> $\text{MatExp} := \text{exponential}(\text{AA}, t)$

$$\text{MatExp} := \begin{bmatrix} \frac{2e^{-2t}}{3} + \frac{e^{4t}}{3} & \frac{e^{4t}}{6} - \frac{e^{-2t}}{6} \\ \frac{4e^{4t}}{3} - \frac{4e^{-2t}}{3} & \frac{e^{-2t}}{3} + \frac{2e^{4t}}{3} \end{bmatrix} \quad (46)$$

> $\text{SolHom} := \text{evalm}(\text{MatExp} \& * \text{Xcero})$

$$\text{SolHom} := \begin{bmatrix} -\frac{7e^{4t}}{6} + \frac{7e^{-2t}}{6} & -\frac{7e^{-2t}}{3} - \frac{14e^{4t}}{3} \end{bmatrix} \quad (47)$$

> $\text{SolHomCero} := \text{map}(\text{rrecurry}(\text{eval}, t=0'), \text{SolHom})$

$$\text{SolHomCero} := \begin{bmatrix} 0 & -7 \end{bmatrix} \quad (48)$$

> $\text{MatExpTau} := \text{map}(\text{rcurry}(\text{eval}, t='t - \text{tau}'), \text{MatExp})$

$$\text{MatExpTau} := \begin{bmatrix} \frac{2 e^{-2t+2\tau}}{3} + \frac{e^{4t-4\tau}}{3} & \frac{e^{4t-4\tau}}{6} - \frac{e^{-2t+2\tau}}{6} \\ \frac{4 e^{4t-4\tau}}{3} - \frac{4 e^{-2t+2\tau}}{3} & \frac{e^{-2t+2\tau}}{3} + \frac{2 e^{4t-4\tau}}{3} \end{bmatrix} \quad (49)$$

> $\text{BBtau} := \text{map}(\text{rcurry}(\text{eval}, t='tau'), \text{BB})$

$$\text{BBtau} := \begin{bmatrix} 0 & 6 e^{-2\tau} \end{bmatrix} \quad (50)$$

> $\text{ProdTau} := \text{simplify}(\text{evalm}(\text{MatExpTau} \& * \text{BBtau}))$

$$\text{ProdTau} := \begin{bmatrix} (e^{4t-4\tau} - e^{-2t+2\tau}) e^{-2\tau} & 2 (e^{-2t+2\tau} + 2 e^{4t-4\tau}) e^{-2\tau} \end{bmatrix} \quad (51)$$

> $\text{SolNoHom} := \text{map}(\text{int}, \text{ProdTau}, \text{tau} = 0 .. t)$

$$\text{SolNoHom} := \begin{bmatrix} \frac{e^{4t}}{6} - \frac{e^{-2t}}{6} - t e^{-2t} & \frac{2 e^{4t}}{3} + 2 t e^{-2t} - \frac{2 e^{-2t}}{3} \end{bmatrix} \quad (52)$$

> $\text{SolPartFinal} := \text{evalm}(\text{SolHom} + \text{SolNoHom}) : y[1](t) = \text{SolPartFinal}[1]; y[2](t) = \text{SolPartFinal}[2]$

$$y_1(t) = -e^{4t} + e^{-2t} - t e^{-2t}$$

$$y_2(t) = -3 e^{-2t} - 4 e^{4t} + 2 t e^{-2t} \quad (53)$$

> $\text{simplify}(\text{SolPart})$

$$y(t) = -e^{4t} + e^{-2t} - t e^{-2t} \quad (54)$$

> restart

6)

> $\text{Ecua} := \text{diff}(y(t), t\$2) - 4 \cdot \text{diff}(y(t), t) + 6 \cdot y(t) = 30 \cdot \text{Heaviside}(t - \text{Pi})$

$$\text{Ecua} := \frac{d^2}{dt^2} y(t) - 4 \frac{d}{dt} y(t) + 6 y(t) = 30 \text{Heaviside}(t - \pi) \quad (55)$$

> $\text{CondIni} := y(0) = 0, D(y)(0) = 0$

$$\text{CondIni} := y(0) = 0, D(y)(0) = 0 \quad (56)$$

> $\text{with}(\text{inttrans}) :$

> $\text{EcuaTL} := \text{subs}(\text{CondIni}, \text{laplace}(\text{Ecua}, t, s))$

$$\text{EcuaTL} := s^2 \mathcal{L}(y(t), t, s) - 4 s \mathcal{L}(y(t), t, s) + 6 \mathcal{L}(y(t), t, s) = \frac{30 e^{-s\pi}}{s} \quad (57)$$

> $\text{SolTL} := \text{isolate}(\text{EcuaTL}, \text{laplace}(y(t), t, s))$

$$\text{SolTL} := \mathcal{L}(y(t), t, s) = \frac{30 e^{-s\pi}}{s (s^2 - 4s + 6)} \quad (58)$$

> $\text{SolPart} := \text{invlaplace}(\text{SolTL}, s, t)$

$$\text{SolPart} := y(t) = 5 \text{Heaviside}(t - \pi) \left(1 + \left(\sin(\sqrt{2} (t - \pi)) \sqrt{2} - \cos(\sqrt{2} (t - \pi)) \right) e^{-2\pi+2t} \right) \quad (59)$$

> Ecu

$$\frac{d^2}{dt^2} y(t) - 4 \frac{d}{dt} y(t) + 6 y(t) = 30 \text{ Heaviside}(t - \pi) \quad (60)$$

> Comprobacion := simplify(eval(subs(y(t) = rhs(SolPart), Ecu)))

$$\text{Comprobacion} := 30 \text{ Heaviside}(t - \pi) = 30 \text{ Heaviside}(t - \pi) \quad (61)$$

> restart

7)

> Ecu := diff(y(t), t\$2) - 2*diff(y(t), t) + 5*y(t) = 8*exp(t)

$$\text{Ecu} := \frac{d^2}{dt^2} y(t) - 2 \frac{d}{dt} y(t) + 5 y(t) = 8 e^t \quad (62)$$

> CondIni := y(0) = 2, D(y)(0) = 12

$$\text{CondIni} := y(0) = 2, D(y)(0) = 12 \quad (63)$$

> with(inttrans) :

> EcuTL := subs(CondIni, laplace(Ecu, t, s))

$$\text{EcuTL} := s^2 \mathcal{L}(y(t), t, s) - 8 - 2s - 2s \mathcal{L}(y(t), t, s) + 5 \mathcal{L}(y(t), t, s) = \frac{8}{s-1} \quad (64)$$

> SolTL := isolate(EcuTL, laplace(y(t), t, s))

$$\text{SolTL} := \mathcal{L}(y(t), t, s) = \frac{\frac{8}{s-1} + 2s + 8}{s^2 - 2s + 5} \quad (65)$$

> SolPart := invlaplace(SolTL, s, t)

$$\text{SolPart} := y(t) = (2 + 5 \sin(2t)) e^t \quad (66)$$

> Comprobacion := simplify(eval(subs(y(t) = rhs(SolPart), Ecu)))

$$\text{Comprobacion} := 8 e^t = 8 e^t \quad (67)$$

> CondicionUno := y(0) = simplify(subs(t=0, rhs(SolPart)))

$$\text{CondicionUno} := y(0) = 2 \quad (68)$$

> CondicionDos := D(y)(0) = simplify(subs(t=0, rhs(diff(SolPart, t))))

$$\text{CondicionDos} := D(y)(0) = 12 \quad (69)$$

> Ecu

$$\frac{d^2}{dt^2} y(t) - 2 \frac{d}{dt} y(t) + 5 y(t) = 8 e^t \quad (70)$$

> CondIni

$$y(0) = 2, D(y)(0) = 12 \quad (71)$$

7b)

> SistemaUno := diff(y[1](t), t) = y[2](t)

$$\text{SistemaUno} := \frac{d}{dt} y_1(t) = y_2(t) \quad (72)$$

> SistemaDos := diff(y[2](t), t) = -5*y[1](t) + 2*y[2](t) + 8*exp(t)

$$\text{SistemaDos} := \frac{d}{dt} y_2(t) = -5 y_1(t) + 2 y_2(t) + 8 e^t \quad (73)$$

$$\begin{aligned} > AA := \text{array}([[0, 1], [-5, 2]]) \\ AA &:= \begin{bmatrix} 0 & 1 \\ -5 & 2 \end{bmatrix} \end{aligned} \quad (74)$$

$$\begin{aligned} > Xcero := \text{array}([2, 12]) \\ Xcero &:= [2 \quad 12] \end{aligned} \quad (75)$$

$$\begin{aligned} > BB := \text{array}([0, 8 \cdot \exp(t)]) \\ BB &:= [0 \quad 8 e^t] \end{aligned} \quad (76)$$

> with(linalg) :

$$\begin{aligned} > MatExp := \text{exponential}(AA, t) \\ MatExp &:= \begin{bmatrix} \cos(2t) e^t - \frac{\sin(2t) e^t}{2} & \frac{\sin(2t) e^t}{2} \\ -\frac{5 \sin(2t) e^t}{2} & \cos(2t) e^t + \frac{\sin(2t) e^t}{2} \end{bmatrix} \end{aligned} \quad (77)$$

$$\begin{aligned} > SolHom := \text{evalm}(MatExp \&* Xcero) : y[1](t) = SolHom[1] \\ y_1(t) &= 2 \cos(2t) e^t + 5 \sin(2t) e^t \end{aligned} \quad (78)$$

$$\begin{aligned} > MatExpTau := \text{map}(\text{rcurry}(\text{eval}, t='t - \text{tau}'), MatExp) \\ MatExpTau &:= \end{aligned} \quad (79)$$

$$\begin{bmatrix} \cos(2t - 2\tau) e^{t-\tau} - \frac{\sin(2t - 2\tau) e^{t-\tau}}{2} & \frac{\sin(2t - 2\tau) e^{t-\tau}}{2} \\ -\frac{5 \sin(2t - 2\tau) e^{t-\tau}}{2} & \cos(2t - 2\tau) e^{t-\tau} + \frac{\sin(2t - 2\tau) e^{t-\tau}}{2} \end{bmatrix}$$

$$\begin{aligned} > BBtau := \text{map}(\text{rcurry}(\text{eval}, t='tau'), BB) \\ BBtau &:= [0 \quad 8 e^\tau] \end{aligned} \quad (80)$$

$$\begin{aligned} > ProdTau := \text{evalm}(MatExpTau \&* BBtau) \\ ProdTau &:= \left[4 \sin(2t - 2\tau) e^{t-\tau} e^\tau \quad 8 \left(\cos(2t - 2\tau) e^{t-\tau} + \frac{\sin(2t - 2\tau) e^{t-\tau}}{2} \right) e^\tau \right] \end{aligned} \quad (81)$$

$$\begin{aligned} > SolNoHom := \text{simplify}(\text{map}(\text{int}, ProdTau, \text{tau} = 0 .. t)) \\ SolNoHom &:= [4 \sin(t)^2 e^t \quad 4 \sin(t) (\sin(t) + 2 \cos(t)) e^t] \end{aligned} \quad (82)$$

$$\begin{aligned} > SolPartFinal := \text{simplify}(\text{evalm}(SolHom + SolNoHom)) \\ SolPartFinal &:= [2 e^t + 10 e^t \sin(t) \cos(t) \quad 2 (5 \sin(t) \cos(t) + 10 \cos(t)^2 - 4) e^t] \end{aligned} \quad (83)$$

$$\begin{aligned} > y[1](t) = SolPartFinal[1] \\ y_1(t) &= 2 e^t + 10 e^t \sin(t) \cos(t) \end{aligned} \quad (84)$$

$$\begin{aligned} > \text{expand}(SolPart) \\ y(t) &= 2 e^t + 10 e^t \sin(t) \cos(t) \end{aligned} \quad (85)$$

$$> y[2](t) = \text{expand}(SolPartFinal[2])$$

$$y_2(t) = 10 e^t \sin(t) \cos(t) + 20 e^t \cos(t)^2 - 8 e^t \quad (86)$$

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> CondUno := y[1](0) = simplify(subs(t=0, SolPartFinal[1]))
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$$CondUno := y_1(0) = 2 \quad (87)$$

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> ConmdDos := y[2](0) = simplify(subs(t=0, SolPartFinal[2]))
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$$ConmdDos := y_2(0) = 12 \quad (88)$$

```
> CondIni
```

$$y(0) = 2, D(y)(0) = 12 \quad (89)$$

```
> restart
```

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8)
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> h := exp(t)·Heaviside(t - Pi)
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$$h := e^t \text{Heaviside}(t - \pi) \quad (90)$$

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> with(inttrans) :
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> H := laplace(h, t, s)
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$$H := \frac{e^{-\pi(s-1)}}{s-1} \quad (91)$$

```
> restart
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9a) Obtenga
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> f := t·Dirac(t - 1) + Heaviside(t - 3)
```

$$f := t \text{Dirac}(t - 1) + \text{Heaviside}(t - 3) \quad (92)$$

```
> with(inttrans) :
```

```
> F := laplace(f, t, s)
```

$$F := e^{-s} + \frac{e^{-3s}}{s} \quad (93)$$

```
> G := \frac{s \cdot \exp(-3s)}{(s^2 + 4s + 5)}
```

$$G := \frac{s e^{-3s}}{s^2 + 4s + 5} \quad (94)$$

```
> g := invlaplace(G, s, t)
```

$$g := \text{Heaviside}(t - 3) e^{-2t+6} (\cos(t - 3) - 2 \sin(t - 3)) \quad (95)$$

```
> restart
```

```
FINAL SERIE 3
```

```
>
```